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**International Asset Allocation with Time-Varying Investment Opportunities***

I. Introduction

*It is worth setting out once again why London’s global managers have been so sceptical of Wall Street in the 1990s. But more fundamentally, what 1997 has shown so clearly, not just in the US, is that when value managers lose control of their markets they can flounder for extended periods. Investor attitudes were formed in the 1980s when the US stock market was the worst performing of the major global markets. The US was written off by many foreigners as slow-growing and inefficient, albeit with an interesting technology sector. (Barry Riley, Financial Times, December 16, 1997)*

This paper investigates the extent of and rewards to institutional investors’ market-timing

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activity by analyzing a panel of 247 U.K. pension funds’ foreign equity holdings in four regional markets (Japan, North America, Europe, and Asia-Pacific) over the period 1991 to 1997. The advantage of working with data on U.K. pension funds is that they face very few restrictions on their investment behavior. We find evidence of extensive attempts at market timing. At first, this seems unsurprising since it is well known that British funds persistently bet against the U.S. stock market during the 1990s, not just by initially underweighting U.S. stocks, but also by systematically reducing their U.S. investments during a period when the global weight of the U.S. stock market rose substantially. More surprising, perhaps, are the drivers behind international asset allocation decisions. We find strong evidence that a substantial portion of the market-timing activity of individual funds can be explained by time-varying expected returns, volatilities, and covariances in the four regions we investigate. In particular, the observed decline in allocation to the North American stock market coincided with a systematic decline over the sample period in expected returns on North American assets relative to those from other developed markets, even though ex post the realized returns in this market were very high.

Studying individual funds’ investment decisions turns out to have many advantages. Bohn and Tesar (1996) were among the first to draw attention to the importance of expected returns for international capital flows. However, they studied aggregate flows for U.S. investors and found only limited empirical support for the proposition that expected returns could explain portfolio flows. Since the composition of aggregate capital flows is unlikely to remain stable over time, such findings can be difficult to interpret. In fact, we find that time-varying expected returns are more important at the level of individual institutional investors’ asset allocation decisions than in the aggregate. In portfolio-weight regressions, a remarkable 94 and 98% of all funds generated a positive and significant coefficient on expected returns for North America and Europe, respectively. These regions account for more than 75% of the funds’ international equity holdings. In an attempt to capture international diversification effects, we include conditional own-market volatility and conditional covariances with domestic returns as additional explanatory variables. The percentage of funds that generated a negative coefficient on either own-market volatility or conditional covariance with global stock returns varied from 48% (Europe) to 98% (Japan). These results indicate that time-varying conditional moments are essential for explaining and evaluating institutional investors’ international asset allocations.

The withdrawal of funds from North America together with the fact that the U.S. stock market paid substantially higher returns than other major developed markets during the sample period might lead one to conclude that returns from international market timing were negative.
simply as a result of this one major market-timing bet.\textsuperscript{1} Compared with a strategy of using global market capitalization weights for their foreign equity portfolio, U.K. pension funds were a massive 29 percentage points underweight in North America over the sample period. Since the average return on North America was more than 10 percentage points above the average international return for other developed markets, a negative mean return of around 3\% per annum from this decision is suggested. However, this conclusion may be premature since it confuses ex post returns with ex ante expected performance. The decision to withdraw from North America appears to have been the result of low or even negative expected returns resulting from rising stock valuations and low dividend yields in this market. So, it is possible that U.K. funds possessed market-timing skills over and above that which could have been inferred from a model of expected returns based on public information. We argue that a valid assessment of market-timing skills has to be conducted in the context of a conditional analysis that allows for time-varying investment opportunities.

We investigate the market-timing skills of the pension funds using a battery of tests that account for a time-varying investment opportunity set. While the importance of time-varying investment opportunities is widely acknowledged in studies of domestic fund performance, to our knowledge, no study has previously investigated these effects in the context of international asset allocation. Once we control for the effects of public information, there is no evidence of what Graham and Harvey (1996) refer to as extra-market-timing ability, that is, anticipating return movements beyond that which could have been predicted using public information. Our estimates indicate that the median fund earned a negative return from international market timing of around \(-0.2\) percent per annum.

The plan of the paper is as follows. Section II provides a description and initial characterization of our data set. Section III analyzes the extent to which the funds’ investment strategies in foreign markets can be explained by time variations in the investment opportunity set. Section IV examines evidence on returns from the part of international market timing not explained by time-varying investment opportunities, and section V concludes.

II. Data

Our data consists of monthly observations on 247 U.K. pension funds’ investments in international equities over the period 1991:1–97:12. It

\textsuperscript{1} For example, in his \textit{Financial Times} column of December 16, 1997, Barry Riley wrote “The latest revival on Wall Street... has further inflamed the wounds of the overseas managers who have been so underweight in US equities all year.” In his column of May 13, 1998, under the heading “Wall Street Misread,” Riley wrote that “Last year’s huge underweighting [of the U.S. market] is being blamed on strategists’ poor judgement.”
was provided to us by The WM Company of Edinburgh, U.K. The sample is complete in the sense that it contains all the funds that maintained the same single, externally appointed fund management group throughout the period and reported their performance data continuously to WM over the period.

The fact that we consider only funds with the same manager in place over the sample period raises the possibility that our sample is subject to survivor bias. Fortunately, this bias is likely to be very small: a comparison of the mean return on the international equity portfolio of the full set of funds tracked by WM (12.50% per annum) with either the average value-weighted return (12.58%) or the average equal-weighted return (12.51%) on our sample of funds reveals that the difference in mean returns is negligible. The finding of a 7 basis point difference between the equal-weighted and value-weighted returns of pension funds also suggests that there is no significant difference between small and large funds’ average performance. Further confirmation of the similarity between our sample and the full set of funds tracked by WM is provided by a time-series correlation of 0.998 between (value-weighted) returns on the two sets of funds.

For each fund, we have data on four regional constituents: Japan, North America, Europe (excluding the United Kingdom), and Asia-Pacific (excluding Japan). For each region, every fund reports initial market value and net investment, income received, and return over the month. All asset holdings and returns are reported in pounds sterling.

Interest in analyzing international portfolio flows has grown recently. Based on monthly recordings of transactions in long-term marketable securities reported to the U.S. Treasury International Capital system and using similar sources for other countries, Tesar and Werner (1994) analyzed the evolution in aggregate holdings of foreign assets in five major economies. They found, among other things, that investors’ turnover rate in foreign equity investments is high relative to their home market turnover rate. Cooper and Kaplanis (1994) considered market capitalization data but did not discuss portfolio flows. Kang and Stulz (1997) examined foreign investors’ aggregate holdings of individual firms’ stocks. They found that foreign investors are cautious in their choice of assets and predominantly hold the equities of large firms in manufacturing industries as well as the equities of firms with good accounting performance.

2. Some funds also held positions in a sector entitled “other international equities,” which largely consists of African, Middle Eastern, and South American equities as well as mutual funds that could not be allocated exclusively to one of the four main categories. But these holdings were very small, less than 1% of total international equity holdings for much of the sample. Since the data records on this category were found to be incomplete, this sector was dropped entirely from the analysis and the weights rescaled for the four main regions.
Our data set is unique relative to those analyzed in previous studies in that it is organized by individual pension funds’ asset holdings. Froot, O’Connell, and Seasholes (2001) used daily data on international transactions over the period 1994–98 to shed light on the relationship between foreign asset trades and stock returns. Their data consist of detailed records on aggregate holdings of pension, endowment, and mutual funds and of governments. Choe, Kho, and Stulz (1999) examine transactions of foreign investors on the Korea Stock Exchange over the period November 1996–December 1997. While our data set is not well suited to studying the price impact of foreign investors in a particular domestic market, it is ideally suited for analyzing institutional investors’ reallocations of funds across major developed capital markets and hence allows us to characterize and quantify the investment strategy of a key group of investors. Although our sample period is relatively short, this has certain advantages. As Tesar and Werner (1994) and Kang and Stulz (1997) point out, barriers to international investment have been declining over the last 20–30 years and our post-1980s data set is unlikely to be contaminated by this relaxation of capital controls.

A first impression of some key features of our data is provided in figure 1, which plots aggregate portfolio weights in the four regions against the corresponding global market capitalization weights. The figure shows that U.K. pension funds’ total international portfolio weights vary considerably over time. The aggregate weights in Japan, for example, increased by almost 8 percentage points in 1991, only to more than halve from 25 to 11% between 1992 and 1994. They more than doubled in early 1994, then drifted back again between 1995 and 1997. Over the full sample period, there is little overall change in the portfolio weight for Japan.

Turning to North America, a very different picture emerges. The weights decreased almost consistently throughout the sample period, from an initial level of 28% in early 1991 to around 10% at the end of 1996. Despite a slight increase to 14% by the end of the sample period, this cannot hide the massive withdrawal of U.K. pension funds from North American equities at a rate in excess of 200 basis points per year.

Unsurprisingly, European equities account for around half of U.K. pension funds’ international equity holdings. This weight increased over the sample period, particularly from 1996 to the end of 1997, when it rose from 39 to 57% of total foreign equity holdings. For the whole sample period, the weights increased considerably from 20% in 1991 to around 40% at the end of 1997. Despite a slight increase to 48% by the end of the sample period, this cannot hide the massive withdrawal of U.K. pension funds from North American equities at a rate in excess of 200 basis points per year.

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Fig. 1.—U.K. pension funds’ portfolio weights and global market weights (percentages)
period, the average annual increase in the weight in Europe amounted to 179 basis points. The weight in Asia-Pacific excluding Japan (Asia-Pacific, for short) rose consistently over most of the period, almost tripling from 10 to 28% of the total from 1991 to the end of 1995. In 1996 and 1997, investments in this region dropped sharply to around 12%, however, as a result of the Asia-Pacific economic crisis.

Several interesting features emerge from comparing these weights with their global counterparts (rescaled to sum to 100%): (1) At the beginning of the sample, U.K. pension funds had less than half the global weighting in Japanese equities. However, following the drop in both the yen and Japanese stock prices over the decade, this difference had virtually disappeared by the end of 1997. (2) U.K. pension funds were initially underweight in North America by about 15 percentage points (28 versus 43%) and this difference widened steadily during the 1990s. The global weight of the U.S. equity market was close to 60% by the end of 1997, while U.K. funds scaled their holdings of international equities in the North American market back to 14%. Hence, the global weight in North America was an astonishing four times higher than that held by U.K. funds by the end of the sample. (3) U.K. pension funds were overweight in Europe and Asia-Pacific. They held three times the world weight in both Europe and Asia-Pacific at both the beginning and end of the sample. An important conclusion emerges from this behavior: There is no evidence of convergence to the global weights over the sample period (with the possible exception of Japan, and this might be pure coincidence).

Figure 1 also offers the impression that the volatility of U.K. pension funds’ aggregate portfolio weights exceeds those of the global weights (which represents the average global investor’s portfolio). To test this formally, for each month, we computed the variance of the portfolio weight changes across markets (in basis points) both for the global portfolio and for the value-weighted portfolio of U.K. pension funds. The average monthly standard deviation of the pension fund portfolio weights was 104 basis points against 92 basis points for the world portfolio. A one-sided test of the null that these standard deviations are identical against the alternative that U.K. pension funds have greater volatility in portfolio weight changes could be rejected at the 5% critical level.

III. Portfolio Weights and Time-Varying Investment Opportunities

This section addresses the issue of whether the dynamics of portfolio changes reflect time variation in the conditional moments of stock returns in the four regions. To quote Brennan, Schwartz, and Lagnado (1997): “A *sine qua non* of tactical asset allocation is time variation or predictability in expected asset returns” (p. 1378). The theory of mean-variance optimizing investors’ portfolio behavior implies that optimal
portfolio weights should reflect the conditional correlation structure of international asset returns, conditional expected asset returns, and a set of hedge factors (see Solnik 1974; Stulz 1981; and Adler and Dumas 1983). This suggests that U.K. pension funds’ decisions, at least in part, may have been driven by time-varying expected moments of returns.

While there is no consensus on how best to model the conditional moments of asset returns, there is now strong evidence that the investment opportunity set in most countries displays considerable time variation (see Harvey 1991; Bekaert and Hodrick 1992; Campbell and Hamao 1992; and Ferson and Harvey 1993). Return correlations also appear to increase in bear markets (see Erb, Harvey, and Viskanta 1994; Lin, Engle, and Ito 1994; and Longin and Solnik 1995). Some studies suggest that changes in the investment frontier can be permanent. For example, Erb et al. (1994) report an upward trend in the conditional correlation between U.K. stock returns and those of Germany, Italy, France, and the United States. Studies such as Dumas and Solnik (1995) and De Santis and Gerard (1998) find that foreign exchange risk is priced in equilibrium and may vary substantially over time.

We follow the literature, most notably Harvey (1991) and Bohn and Tesar (1996), and model expected returns in each region as a function of a set of commonly used state variables. As instruments we use an intercept term, the default premium \( \text{Def}_t \) on U.S. bonds computed as the differential yield on Baa and Aaa rated bonds, the 1-month U.S. T-bill rate \( I_{US}^t \) and the U.S.–U.K. T-bill spread \( I_{US}^t - I_{UK}^t \). Finally, we include the local dividend yield in each region \( \text{Yield}_{jt} \). These instruments are very similar to those adopted by Harvey, with the exception of the T-bill spread between the U.S. and U.K. markets, which is included to reflect a key information variable from the perspective of U.K. investors.4 All returns are denominated in sterling to reflect the objectives of a U.K. pension fund. Hence, the specification of the conditional mean in our regressions is

\[
    r_{jt+1} = \gamma_0 + \gamma_1 \text{Yield}_{jt} + \gamma_2 \text{Def}_t + \gamma_3 I_{US}^t + \gamma_4 (I_{US}^t - I_{UK}^t) + \eta_{jt+1}.
\]

To capture possible time variations in conditional volatilities and covariances, we model returns in the context of a bivariate generalized ARCH model. The contribution of foreign equity holdings to a pension fund’s total volatility from foreign equity holdings is determined in part

4. Returns and dividend yields were obtained from Morgan Stanley Capital International. The quality spread is based on data from DRI, the U.S. T-bill rate is from the CRSP tapes, while the U.K. T-bill rate is from DataSTREAM.
by their own volatility and in part by their covariance with global returns. Let \( r_{t+1} = (r_{jt+1} r_{wt+1})' \), where \( r_{jt+1} \) and \( r_{wt+1} \) are region \( j \) and global equity returns in month \( t + 1 \), respectively. We follow Bollerslev (1990) and model returns as follows:

\[
    r_{t+1} = \Gamma Z_t + \boldsymbol{\eta}_{t+1},
\]

\[
    \sigma_{kk,t}^2 = \alpha_{kk} + \beta_{k0} \eta_{kk,t}^2 + \beta_{k1} \sigma_{kk,t-1}^2, \quad k, l = j, w,
\]

where \( \boldsymbol{\eta}_{t+1} = (\eta_{jt+1}, \eta_{wt+1})' \) is the set of heteroscedastic return innovations defined as \( \eta_{t+1} = (\varepsilon_{jt+1}, \varepsilon_{wt+1})' \) are normal, independent, and identically distributed residuals so that \( \eta_{t+1} \sim N(0, \Sigma_t) \) where \( \Sigma_t = [\sigma_{kl,t}^2] \) is the conditional covariance matrix and \( \psi_{kl} \) is the conditional correlation coefficient, which is assumed to be constant and was always found to be nonnegative. Finally, \( Z_t = \{ \text{Yield}_{jt}, \text{Def}_t, I_{tUS}^j, I_{tUS}^j - I_{tUK}^j \} \) is a vector of instruments, while \( \Gamma \) is a conformable matrix of regression coefficients. This model generates an estimate of the expected returns and conditional volatility of returns in each region as well as its conditional covariance with global equity returns.

Table 1 reports the output from these regressions estimated on data over the sample 1970:1 to 1997:12. The default premium variable is highly significant with a positive coefficient in all regions, while the 1-month T-bill rate has a negative and significant coefficient in all regions. Local dividend yields seem to be important only for Asia-Pacific. ARCH effects are strong and volatility persistent in Japan, Asia-Pacific and globally.

Armed with this specification of the time-varying opportunity set, we next investigate the relation between portfolio weights and the expected return in each region, the conditional volatility of the return within the region as well as the region’s conditional covariance with returns on the U.K. stock market. This analysis extends the work by Bohn and Tesar (1996), which focused on conditional means but did not include an estimate of conditional volatility and covariance. Each of the conditional moments was computed in excess of the corresponding average ‘world ex-UK’ moment computed as a capitalization-weighted average across the four regions. We include expected own-market excess returns rather than the separate expected returns for all markets to reduce the number of parameters to be estimated.

5. Let \( \varepsilon_t \) be a \( 4 \times 1 \) vector with unity in the \( j \)th row and zeros elsewhere, let \( \mu_t \) be the vector of expected returns for period \( t \), and let \( \omega_t \) be the vector of world capitalization weights for the four regions under investigation (rescaled to sum to unity). Then expected excess returns in region \( j \) were computed as \( \sigma_{jt}^2 = (\varepsilon_t^j - \omega_t^j) \mu_t \).


<table>
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<th>Japan</th>
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Note.—The table presents maximum likelihood estimates from the following bivariate GARCH model:

\[
\begin{align*}
    r_{jt+1} &= \gamma_0 + \gamma_1 \text{Yield}_j + \gamma_2 \text{Def}_j + \gamma_3 I_{us}^j + \gamma_4 (I_{us}^j - I_{uk}^j) + \eta_{jt+1} \\
    \eta_{jt+1} &= \sigma_{\eta,j} \xi_{jt+1}, \quad \xi_{jt+1} \sim N(0,1) \\
    \sigma_{kl,t}^2 &= \alpha_k + \beta_k \sigma_{kl,t-1}^2 + \beta_{kl} \xi_{kt}^2, \quad k, I = j, w \\
    \sigma_{kl,t} &= \psi_{kl} \sigma_{kl,t-1}^\alpha \sigma_{kl,t}, \quad k, I = j, w
\end{align*}
\]

The model was estimated pairwise on returns in the four regional markets and on the global stock market index. Standard errors are provided in parentheses beside the estimates. The estimations are based on the constant conditional correlation specification proposed by Bollerslev (1990). The regressors are defined as follows: \(r_{jt+1}\) is the return in region \(j\) in period \(t+1\), \(\text{Yield}_j\) is the dividend yield in region \(j\), \(\text{Def}_j\) is the default premium on Baa over Aaa rated bonds, \(I_{us}^j\) is the 1-month U.S. T-bill rate, and \(I_{uk}^j\) is the 1-month U.K. T-bill rate. An asterisk implies significance at the 5% level. The sample covers 247 U.K. pension funds over the period 1991:1–1997:12.
We do not experiment with different specifications but simply use linear projections of portfolio weights on first and second conditional moments as an approximation to a relationship between portfolio weights and conditional moments, which could be both more complex and vary over time. Consistent with theoretical models of intertemporal asset allocation (e.g., Brennan et al. 1997), we use portfolio weights, \( \omega_{ijt} \), as the dependent variables. For each fund, \( i \), and each region, \( j \), we estimate a set of time-series regressions:

\[
\omega_{ijt} = \alpha_{ij} + \sum_{k=1}^{4} \beta_{1ik} \hat{\rho}_{kt} + \sum_{k=1}^{4} \beta_{2ik} \hat{\sigma}_{kk,t} + \sum_{k=1}^{4} \beta_{3ik} \hat{\sigma}_{kw,t} + \varepsilon_{ijt}, \tag{3}
\]

where \( \hat{\rho}_{kt} \) is the expected excess return in region \( k \), while \( \hat{\sigma}_{kk,t} \) is the conditional return volatility and \( \hat{\sigma}_{kw,t} \) is the conditional covariance with global equity returns, all estimated from eq. (2). These moments are based on information at time \( t - 1 \) and, hence, are known by the time the fund decides on \( \omega_{ijt} \). As we shall see, it is important that the same regressors appear in each equation to ensure consistency of the parameter estimates.

For each fund, \( i \), the weights sum to one across the regions, \( j \): \( \sum_{j=1}^{4} \omega_{ijt} = 1 \). \( \tag{4} \)

This means that the coefficients in eq. (3) are subject to the adding-up constraints:

\[
\sum_{k=1}^{4} \alpha_{ik} = 1 \\
\sum_{k=1}^{4} \beta_{1ik} = 0 \\
\sum_{k=1}^{4} \beta_{2ik} = 0 \\
\sum_{k=1}^{4} \beta_{3ik} = 0. \tag{5}
\]

6. Note also that, unlike our model, the stochastic process assumed in the return-generating model in Brennan et al. (1997) assumes constant volatility.

7. In the context of allocation or demand systems, the equivalent condition is that the sum of the individual components equals a predetermined aggregate. This is known as the adding-up criterion (c.f., Bewley 1986).
To see the consequences of these constraints on parameter estimation, we write the full set of constraints on a given fund’s portfolio weights as follows:

$$
W_i \equiv \begin{pmatrix}
\omega_{i11} & \omega_{i21} & \omega_{i31} & \omega_{i41} \\
\omega_{i12} & \omega_{i22} & \omega_{i32} & \omega_{i42} \\
\vdots & \vdots & \vdots & \vdots \\
\omega_{i1T} & \omega_{i2T} & \omega_{i3T} & \omega_{i4T}
\end{pmatrix} = X\beta_i + U_i, \quad (6)
$$

where $X$ is a $T \times p$ matrix of predetermined regressors, $\beta_i$ is a $p \times 4$ matrix of coefficients and $U_i$ is a $T \times 4$ matrix of innovation terms; $p$ is the number of regressors, which in our case equals one plus the number of moments the portfolio weights are projected on.

The system of portfolio weight equations can also be written in the following convenient way:

$$
\text{vec}(W_i) = (I \otimes X)\text{vec}(\beta_i) + \text{vec}(U_i)
$$

$$
E\left[\text{vec}(U_i)\text{vec}(U_i)^T\right] = \Omega_i \otimes I, \quad (7)
$$

where $\text{vec}(\cdot)$ is the vector stacking operator, $\otimes$ is the Kronecker product, $\Omega_i$ is a $4 \times 4$ symmetric covariance matrix, and $I$ is the identity matrix of suitable dimension. Using this notation, the adding-up constraint can be written as follows

$$
W_{i,t4} = X\beta_{i,t4} + U_{i,t4} = t_T, \quad (8)
$$

where $t_{4}$ and $t_T$ are $4 \times 1$ and $T \times 1$ unity vectors, respectively. These constraints have important implications for the estimation of the covariance matrix for the system of portfolio weights. This will be singular since

$$
\Omega_{i,t4} = T^{-1}E\left[U_i'U_i\right]t_4 = T^{-1}E\left[U_i'U_{i,t4}\right] = 0. \quad (9)
$$

More intuitively, this is an implication of the constraint that, at each point in time, $t$, and for each fund, $i$, the innovations must add up to zero:

$$
\sum_{j=1}^{4} \varepsilon_{ijt} = 0. \quad (10)
$$

Standard generalized least squares and maximum likelihood methods can therefore not be used to estimate coefficients in the full system of portfolio weights, eq. (6). Instead, it is necessary to delete one column from eq. (6)
and constrain the estimators. Letting $\Omega_{11i}$ be the $3 \times 3$ covariance matrix of full rank for the first three sets of portfolio weights, while $W_{1i}$ and $\beta_{1i}$ are the first three columns of $W_i$ and $\beta_i$, the log-likelihood function of the subsystem comprising the first three weights is

$$\ln[L(\text{vec}(W_{1i}))] = -\frac{3T}{2} \ln(2\pi) - \frac{T}{2} \ln(|\Omega_{11i}|)$$

$$- \frac{1}{2} \text{tr} \left[ \Omega_{11i}^{-1}(W_{1i} - X\beta_{1i})'(W_{1i} - X\beta_{1i}) \right].$$

(11)

Taking derivatives now yields the following maximum likelihood estimators for $\beta_{1i}$ and $\Omega_{11i}$:

$$\text{vec}(\hat{\beta}_{1i}) = \left[I \otimes (X'X)^{-1}X'\right] \text{vec}(W_{1i})$$

$$\hat{\Omega}_{11i} = (W_{1i} - X\hat{\beta}_{1i})'(W_{1i} - X\hat{\beta}_{1i}) / T,$$

(12)

see Bewley (1986). The estimated coefficients of a particular column in eq. (6) scaled by their standard errors follow a $t$-distribution, although a Wald test of coefficient restrictions across columns will not have a standard distribution.

Table 2 summarizes the empirical results based on these estimators. Panel A projects portfolio weights onto expected returns alone. More than 95% of all funds generated a positive coefficient on expected returns in North America and Europe, while only 29% did so for Japan and 5% for Asia-Pacific. The result for Asia-Pacific may initially seem puzzling but is related to the importance of the dividend yield for this region and its behavior during the Asian crisis of 1997. During 1997, Asian stock prices plummeted and the dividend yield rose sharply. The outcome was both a sharp fall in the Asia-Pacific portfolio weight and an increase in expected returns. Most remarkable perhaps is the fact that 94 and 98% of the expected return coefficients are statistically significant and positive for North America and Europe, respectively. Since these two regions account for around 75% of the total foreign equity holdings of our sample of pension funds, we can conclude that expected return variation is a significant determining factor of the international asset allocation of the vast majority of funds.

We next included conditional volatility as a regressor in the portfolio weight equation. Panel B shows that the majority of funds (in excess of 70% in Japan, North America, and Asia-Pacific) generated negative coefficients on own-market volatility. This indicates that the funds decreased their allocation toward regions whose volatility was expected to go up. Panel C reports the outcome from using expected returns and conditional covariance with global stock returns as regressors.

8. The estimation results are invariant to which column is deleted from eq. (6). The estimated coefficients of the deleted equation can be derived from the adding-up constraints, eq. (5).
<table>
<thead>
<tr>
<th></th>
<th>Japan</th>
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<th>Europe</th>
<th>Asia-Pacific</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>A. Expected Returns</strong></td>
<td></td>
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<td></td>
<td></td>
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<tr>
<td>Median $\hat{\beta}_{1j}$</td>
<td>-5.11</td>
<td>24.82</td>
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<tr>
<td>% of regressions with $\hat{\beta}_{1j} &gt; 0$</td>
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<td>93.93</td>
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<td>.00</td>
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<td>Median $R^2$</td>
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<td>.80</td>
<td>.92</td>
<td>.72</td>
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<tr>
<td><strong>B. Expected Returns and Volatility</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Median $\hat{\beta}_{2j}$</td>
<td>-1.74</td>
<td>-7.9</td>
<td>.30</td>
<td>-1.4</td>
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<tr>
<td>% of regressions with $\hat{\beta}_{2j} &lt; 0$</td>
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<td>88.66</td>
<td>33.20</td>
<td>71.66</td>
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<td>% of regressions with $t_{\hat{\beta}_{2j}} &lt; -2$</td>
<td>74.08</td>
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<td>Median $R^2$</td>
<td>.59</td>
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<td>.63</td>
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<td><strong>C. Expected Returns and Covariance</strong></td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>Median $\hat{\beta}_{3j}$</td>
<td>-3.92</td>
<td>-3.39</td>
<td>.58</td>
<td>1.55</td>
</tr>
<tr>
<td>% of regressions with $\hat{\beta}_{3j} &lt; 0$</td>
<td>89.47</td>
<td>63.97</td>
<td>48.18</td>
<td>14.17</td>
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<tr>
<td>% of regressions with $t_{\hat{\beta}_{3j}} &lt; -2$</td>
<td>80.16</td>
<td>16.60</td>
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<td>Median $R^2$</td>
<td>.61</td>
<td>.84</td>
<td>.79</td>
<td>.78</td>
</tr>
<tr>
<td><strong>D. Expected Returns, Volatility, and Covariance</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Median $\hat{\beta}_{1ij}$</td>
<td>-5.99</td>
<td>25.81</td>
<td>48.67</td>
<td>-3.07</td>
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<td>% of regressions with $\hat{\beta}_{1ij} &gt; 0$</td>
<td>29.15</td>
<td>97.57</td>
<td>98.79</td>
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<tr>
<td>% of regressions with $t_{\hat{\beta}_{1ij}} &gt; 2$</td>
<td>5.67</td>
<td>94.33</td>
<td>93.12</td>
<td>.00</td>
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<tr>
<td>Conditional volatility:</td>
<td></td>
<td></td>
<td></td>
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</tr>
<tr>
<td>Median $\hat{\beta}_{2ij}$</td>
<td>-2.56</td>
<td>-2.06</td>
<td>1.46</td>
<td>-0.72</td>
</tr>
<tr>
<td>% of regressions with $\hat{\beta}_{2ij} &lt; 0$</td>
<td>97.53</td>
<td>89.07</td>
<td>34.82</td>
<td>78.95</td>
</tr>
<tr>
<td>% of regressions with $t_{\hat{\beta}_{2ij}} &lt; -2$</td>
<td>63.97</td>
<td>11.34</td>
<td>5.67</td>
<td>.40</td>
</tr>
<tr>
<td>Conditional covariance:</td>
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<td></td>
</tr>
<tr>
<td>Median $\hat{\beta}_{3ij}$</td>
<td>.96</td>
<td>-.38</td>
<td>-3.06</td>
<td>4.00</td>
</tr>
<tr>
<td>% of regressions with $\hat{\beta}_{3ij} &lt; 0$</td>
<td>28.74</td>
<td>62.13</td>
<td>57.09</td>
<td>17.00</td>
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<tr>
<td>% of regressions with $t_{\hat{\beta}_{3ij}} &lt; -2$</td>
<td>6.48</td>
<td>9.31</td>
<td>12.96</td>
<td>3.24</td>
</tr>
<tr>
<td>% of regressions with $\hat{\beta}<em>{2ij} + \hat{\beta}</em>{3ij} &lt; 0$</td>
<td>85.83</td>
<td>98.38</td>
<td>53.44</td>
<td>14.98</td>
</tr>
<tr>
<td>% of regressions with $t_{\hat{\beta}<em>{2ij} + \hat{\beta}</em>{3ij}} &lt; -2$</td>
<td>1.21</td>
<td>26.32</td>
<td>11.74</td>
<td>2.83</td>
</tr>
<tr>
<td>Median $R^2$</td>
<td>.66</td>
<td>.86</td>
<td>.82</td>
<td>.70</td>
</tr>
</tbody>
</table>
Conditional covariances are not quite as important as own-market volatility, but they predominantly have the right sign for the three main regions: Japan, North America, and Europe. 9

Panel D shows the results from regressions that include all three explanatory variables. Own-market expected returns continue to have the right sign and be statistically significant for almost all funds’ weights in North America and Europe. Likewise, own-market conditional volatility generates a negative coefficient estimate for the majority of funds, while conditional covariance with global returns produces a negative coefficient estimate for around 60% of the funds in the two largest markets, North America and Europe. However, the sign of the coefficients of some of the volatility and covariance regressors is now difficult to interpret since the two series are driven by a common component and hence strongly correlated. While the individual coefficient estimates

9. In a panel analysis of equity flows, Portes and Rey (1999) found that equity flows between pairs of countries do not seem to be determined by the correlation between equity returns in the two countries, while the volatility of returns in the two markets does matter. Our findings suggest that conditional covariances between returns in the host and foreign country indeed influence portfolio holdings. The difference between these findings may be explained by our use of time-varying conditional moments.

### TABLE 2 (Continued)

<table>
<thead>
<tr>
<th></th>
<th>Japan</th>
<th>North America</th>
<th>Europe</th>
<th>Asia-Pacific</th>
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<tbody>
<tr>
<td>E. Expected Returns, Volatility, and Covariance</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Expected returns:</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Median $\hat{\beta}_{1ij}$</td>
<td>$-10.72$</td>
<td>$30.74$</td>
<td>$32.18$</td>
<td>$-2.47$</td>
</tr>
<tr>
<td>% of regressions with $\hat{\beta}_{1ij} &gt; 0$</td>
<td>$17.00$</td>
<td>$96.36$</td>
<td>$98.79$</td>
<td>$10.53$</td>
</tr>
<tr>
<td>% of regressions with $t_{1ij} &gt; 2$</td>
<td>$5.26$</td>
<td>$91.90$</td>
<td>$95.14$</td>
<td>$4.05$</td>
</tr>
<tr>
<td>Conditional volatility:</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Median $\hat{\beta}_{2ij}$</td>
<td>$3.00$</td>
<td>$-19.97$</td>
<td>$-9.13$</td>
<td>$-1.16$</td>
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<tr>
<td>% of regressions with $\hat{\beta}_{2ij} &lt; 0$</td>
<td>$23.89$</td>
<td>$70.04$</td>
<td>$94.33$</td>
<td>$74.90$</td>
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<tr>
<td>% of regressions with $t_{2ij} &lt; -2$</td>
<td>$6.89$</td>
<td>$47.78$</td>
<td>$40$</td>
<td>$14.17$</td>
</tr>
<tr>
<td>Conditional covariance:</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>% of regressions with $\hat{\beta}_{ijk} &lt; 0$</td>
<td>$85.02$</td>
<td>$19.43$</td>
<td>$15.38$</td>
<td>$41.30$</td>
</tr>
<tr>
<td>% of regressions with $t_{ijk} &lt; -2$</td>
<td>$22.27$</td>
<td>$0$</td>
<td>$0$</td>
<td>$6.47$</td>
</tr>
<tr>
<td>Median $R^2$</td>
<td>$.76$</td>
<td>$.86$</td>
<td>$.77$</td>
<td>$.84$</td>
</tr>
</tbody>
</table>

Note.—Panels A-D of this table reports statistics characterizing the cross-sectional distribution of regression coefficients from linear projections of individual funds’ portfolio weights ($w_{ijt}$) on expected excess returns ($\hat{r}_{kt}$), conditional volatility ($\hat{s}_{kk,t}$), and conditional covariances ($\hat{s}_{kw,t}$) with global stock returns:

$$
\omega_{ijt} = \alpha_{ij} + \sum_{k=1}^{4} \beta_{1ik} \hat{r}_{kt} + \sum_{k=1}^{4} \beta_{2ik} \hat{s}_{kk,t} + \sum_{k=1}^{4} \beta_{3ik} \hat{s}_{kw,t} + \epsilon_{ijt}
$$

Panel E is based on the specification

$$
\omega_{ijt} = \alpha_{ij} + \sum_{k=1}^{4} \beta_{1ik} \hat{r}_{kt} + \sum_{j=1}^{4} \sum_{k=1}^{4} \beta_{2ijk} \hat{s}_{jk,t} + \epsilon_{ijt},
$$

where $\hat{s}_{jk,t}$ is the conditional covariance between returns in regions $j$ and $k$. The sample covers 247 U.K. pension funds over the period 1991:1–97:12.

Conditional covariances are not quite as important as own-market volatility, but they predominantly have the right sign for the three main regions: Japan, North America, and Europe. 9

Panel D shows the results from regressions that include all three explanatory variables. Own-market expected returns continue to have the right sign and be statistically significant for almost all funds’ weights in North America and Europe. Likewise, own-market conditional volatility generates a negative coefficient estimate for the majority of funds, while conditional covariance with global returns produces a negative coefficient estimate for around 60% of the funds in the two largest markets, North America and Europe. However, the sign of the coefficients of some of the volatility and covariance regressors is now difficult to interpret since the two series are driven by a common component and hence strongly correlated. While the individual coefficient estimates

9. In a panel analysis of equity flows, Portes and Rey (1999) found that equity flows between pairs of countries do not seem to be determined by the correlation between equity returns in the two countries, while the volatility of returns in the two markets does matter. Our findings suggest that conditional covariances between returns in the host and foreign country indeed influence portfolio holdings. The difference between these findings may be explained by our use of time-varying conditional moments.
are difficult to interpret, one would expect that the total effect of the own-market variance and covariance with the global market return is negative. We therefore tested whether the sum of the coefficients on own-market variance and covariance with the global market return, $\beta_{2ij} + \beta_{3ij}$, are negative. The results, reported at the bottom of Panel D, show that the total effect of these variables is predominantly negative for the three main regions, Japan, North America, and Europe.

So far the results capture covariance effects by modeling the portfolio weights as a function of the conditional covariances between regional and global market returns. Such covariances represent the regional equity holdings’ contribution to systematic risk in the context of a single-factor international Capital Asset Pricing Model. These covariances are likely to capture a large fraction of the regional returns’ contribution to total portfolio risk. However, since the pension funds hold significant parts of their portfolios in foreign equity, the interregional return covariances also contribute to the total portfolio risk. To investigate the effect of the interregional covariances, we obtained conditional covariance estimates that were used in the following linear regressions:

$$w_{ijt} = \alpha_{ij} + \sum_{k=1}^{4} \beta_{1ik}\hat{r}_{kt} + \sum_{j=1}^{4} \sum_{k=1}^{4} \beta_{2jk}\hat{\sigma}_{jk,t} + \varepsilon_{ijt}. \quad (13)$$

Here $\hat{\sigma}_{jk,t}$ is the conditional covariance between returns in regions $j$ and $k$. The results from these regressions are shown in panel E of table 2. They are similar to those obtained in panel D. For North America and Europe, the vast majority of funds continue to have a positive coefficient on the own-market expected return and a negative coefficient on the own-market volatility, while Japan and Asia-Pacific produce weaker results. The effect of the interregional covariances, computed as $\sum_{k\neq j} \hat{\beta}_{2ijk}$, is negative for the vast majority of funds’ investments in Japan. A negative effect is also observed for close to half the funds in Asia-Pacific. In contrast, there is not much of a negative effect for North America and Europe. Again these results are related to the findings for the conditional variances, since Japan and Asia-Pacific are the regions where own-market volatility has no strong effect on the portfolio weights (but conditional covariances do), while for North America and Europe own-market volatility has a strong negative effect on portfolio weights but the conditional covariances do not.

To further investigate whether information on variances and covariances help predict variation in asset weights, we undertook the predictive information test proposed by Diebold and Mariano (1995). To do so, we first computed the squared forecast error differential, $\text{dif}_i = e_{i*}^2 - e_i^2$, where $e_{i*}$ is the forecast error (i.e., the difference between the actual and predicted weight) based on the full model, eq. (3), that includes time-varying first and second moments, while $e_i$ is the forecast error from a simpler model that projects portfolio weights only on
a constant and expected returns. Based on these forecast errors, we computed the statistic \( \sqrt{T \overline{\text{diff}} / sd(\text{diff})} \), where \( \overline{\text{diff}} = \sum_{t=1}^{T} \text{diff}_t / T \) and \( sd(\text{diff}) \) are estimates of the mean and standard deviation of \( \text{diff}_t \), respectively. This gives a test statistic that is asymptotically normally distributed. The results showed that adding second-moment information led to a significantly better forecast for 22, 19, 72, and 2% of the funds’ weights in Japan, North America, Europe, and Asia Pacific, respectively.

To demonstrate graphically the importance to the evolution in portfolio weights of the time variation in conditionally expected returns, volatilities, and covariances, figure 2 shows the cross-sectional distribution of \( R^2 \) values from these regressions performed for each fund. The \( R^2 \) values are high in all four regions with medians of 0.59 in North America, 0.70 in Asia, 0.48 in Japan, and 0.29 in Europe.\(^{10}\)

We finally computed the optimal portfolio weights based on the first- and second-moment estimates and compared these with the observed portfolio weights. For a mean-variance optimizing investor the optimal portfolio weight on the \( j \)th security is given by (see Bohn and Tesar 1996)

\[
\omega^*_j = \alpha e_j \sum_{t}^{-1} \mu_t + \eta_j,
\]

where \( \alpha \) is the investor’s coefficient of relative risk aversion, \( e_j \) is a zero-one vector selecting the \( j \)th regional return, \( \sum_{t} \) is the conditional covariance matrix between the regional returns, \( \mu_t \) is the vector of expected returns, and \( \eta_j \) represents a ‘hedge factor’ that captures risks beyond those captured by the regional return processes. These are likely to be important here and may represent the (unmodeled) effect of asset-liability matching. Since we do not observe this hedge factor and do not know the true value of \( \alpha \), we simply test the broad implications of the model that there should be a positive correlation between the observed weights (\( \omega_j \)) and the optimal portfolio weights (\( \omega^*_j \)). As it turns out, our results closely match those found in table 2. For the two largest markets, North America and Europe, we found a positive correlation between the observed weights and the optimal weights for 91 and 56% of the funds, respectively. For Japan and Asia-Pacific, we did not find a positive correlation between the actual and optimal portfolio weights for many funds. This is not surprising in light of the zero or negative coefficient on the mean return for most of the funds’ investments in these two regions, see panel D in table 2.

\(^{10}\) Brennan and Cao (1997) conclude that their model, based on lagged returns, “is able to explain only a small portion of the variance of international equity flows” (p. 1876). To explore the relative importance to portfolio weights of time variations in expected returns and second moments relative to past returns, we also estimated regressions that include the most recent returns. The median \( R^2 \) increased only marginally from between 0.00 to 0.02 for the four regions, suggesting that time-varying conditional moments, rather than lagged returns, are more important for explaining individual funds’ asset allocation decisions.
Fig. 2.—Histogram of $R^2$ from regressions of portfolio weights on conditional moments (percentages).
Once again it is interesting to compare these findings with the results in Bohn and Tesar (1996). In regressions of net purchases of foreign equity on predicted excess returns in a cross-section of countries, Bohn and Tesar found that expected excess returns were statistically significant and positively correlated with net purchases in roughly a third of the countries they examined. It is difficult to compare directly their findings on aggregate flows with our results on individual funds since they do not report $R^2$ statistics and do not include time-varying second moments. Nevertheless, the fact that expected returns matter to almost all funds in at least one market (North America) suggests that time-varying expected moments may be even more important at the level of individual institutional investors’ asset allocation decisions than in the aggregate.

IV. Returns from International Market Timing

A. Unconditional Return Performance

To assess the performance of the funds in its stable, WM uses a range of value-weighted asset-class benchmarks. As external benchmarks it employs Financial Times/Standard & Poor (FT/S&P) indices, both of which assume that income is reinvested (gross of tax). However, it is far from obvious which external index provides the more-suitable representation of benchmark returns: Kang and Stulz (1997), for example, show that foreign investors’ holdings of Japanese equities are concentrated in the largest firms.

Figure 3 plots time series of monthly returns on the value-weighted portfolio of funds included in our sample. Also shown in the figure are returns on the corresponding FT/S&P indices. The series are clearly strongly correlated. This impression is confirmed by the sample correlations reported in the last row of table 3. Estimated time-series correlations between the FT/S&P indices and the returns on the value-weighted portfolio of pension funds exceed 0.97 and are as high as 0.99. In light of these high correlations, we do not consider alternative candidates for benchmark returns.

Table 3 also reveals large variations across markets in the individual funds’ mean returns and volatilities relative to the external indices. First, consider the mean returns. For Japan, the value-weighted sample mean return was 2.85% over the period, while the corresponding FT/S&P index paid an average of –0.73% per annum. However, this region is the only one in which a typical U.K. pension fund earned a higher mean return than the benchmark index. In the other regions, the pension funds underperformed the FT/S&P index on a raw return basis by an average

11. The apparent exceptional outperformance in the Japanese stock market can be explained as follows. Although there are no legal constraints on foreign holdings in Japanese bank stocks, U.K. pension funds were underweight in the Japanese banking sector as a result
Fig. 3.—Time-series of proportionate returns on FT/S&P indices and on U.K. pension funds.
of 0.43 (North America), 0.50 (Europe), and 2.06 (Asia-Pacific) percentage points per annum.\(^\text{12}\) For the total international equity portfolio, U.K. pension funds underperformed by 0.70 percentage points per annum an index formed by weighting the four regions’ FT/S&P returns by their international market shares: only 13\% of the funds outperformed the passive world market portfolio.

**B. Conditional Market-Timing Tests**

To test whether U.K. pension funds possess market-timing skills after controlling for public information, we ran a range of tests inspired by Graham and Harvey (1996). Their regressions were designed to measure the market-timing skills of newsletters recommending stocks versus cash and hence assume the existence of a single risky asset. Since we consider the allocation between four risky assets, we have to modify these measures. Initially, we regressed returns in each region in excess of the World (ex-UK) return, \(r_{jt+1} = r_{jt+1} - r_{w,t+1}\), on the previous period’s portfolio weight change and the vector of instruments. Excess of the small percentage of this sector’s stock available for public purchase (a consequence of the high degree of cross-holdings in Japanese banking sector equities). This matters because Japanese banks paid exceptionally low returns over the sample period. In a two-factor regression of the funds’ excess returns in Japan on the Japanese stock market index and the banking sector index, only 0.4\% of funds had significantly positive Jensen alpha estimates. The results may also be explained by the fact, documented by Kang and Stulz (1997), that foreigners in the Japanese stock market tend to hold the equities of large firms. During the 1990s, large Japanese firms paid higher returns than small firms. When we controlled for a capitalization factor, we found once again that only a small portion of the funds generated statistically significant outperformance.

\(^{12}\) These differences show up clearly in the proportion of funds that outperformed the indices on a raw return basis: 97\% of funds outperformed the index in Japanese equities, while only 20, 21, and 9\% of the funds outperformed the FT/S&P indices in North America, Europe, and Asia-Pacific, respectively.

### TABLE 3 Summary Statistics for International Equity Returns

<table>
<thead>
<tr>
<th></th>
<th>Japan</th>
<th>North America</th>
<th>Europe</th>
<th>Asia-Pacific</th>
<th>World ex UK</th>
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</thead>
<tbody>
<tr>
<td>Mean Return (% per year)</td>
<td>FT/S&amp;P index</td>
<td>0.73</td>
<td>20.02</td>
<td>16.50</td>
<td>13.46</td>
</tr>
<tr>
<td></td>
<td>Sample (value weighted)</td>
<td>2.85</td>
<td>19.60</td>
<td>16.00</td>
<td>11.40</td>
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<td></td>
<td>Sample (equal weighted)</td>
<td>3.23</td>
<td>19.21</td>
<td>15.93</td>
<td>11.31</td>
</tr>
<tr>
<td>Percent of outperformers relative to FT/S&amp;P index</td>
<td>97.2</td>
<td>20.2</td>
<td>20.7</td>
<td>8.9</td>
<td>13.27</td>
</tr>
<tr>
<td>Correlation (FT/S&amp;P index, sample)</td>
<td>.977</td>
<td>.993</td>
<td>.989</td>
<td>.989</td>
<td>.924</td>
</tr>
</tbody>
</table>

\textit{Note.}—For each of the four regions under consideration this table reports the mean return (annual percentage) for the Financial Times/Standard & Poor index and the value- and equal-weighted portfolios comprising the funds in our sample. We also report the proportion of outperformers relative to the index and the correlation between the time series of monthly returns on the indices and on the value-weighted portfolios for each of the regions. The sample covers 247 U.K. pension funds over the period 1991:1–97:12.

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returns relative to the average foreign market are used in the regression since expected-return-maximizing funds ought to increase allocations to regions with above-average expected returns:

\[ \rho_{jt+1} = c_j + \beta_{ij} \Delta \omega_{jt} + \beta_j' Z_t + \epsilon_{jt+1} \]  

This regression tests whether funds successfully change their portfolio weights in anticipation of future relative returns in the various markets, after controlling for the publicly known state variables, \( Z_t \), considered in eq. (2). Market-timing skills should show up in the form of a positive coefficient estimate, \( \beta_{ij} \).

Panel A of table 4 shows that on this measure there is some evidence that U.K. investors possessed market-timing skills: the median estimate of \( \beta_{ij} \), computed across individual funds, is positive for three out of four regions, the exception, not surprisingly, being North America. Furthermore, the percentage of funds with positive estimates of market-timing skills is very high in Japan (91% of all funds), Asia (89%), and relatively high in Europe (61%). In contrast, only 30% of funds obtained a positive market-timing coefficient for North America. However, the percentage of funds with estimates of \( \beta_{ij} \) that are statistically significant and positive at the 5% level is quite low (below 6% in all regions).

In the presence of multiple risky assets, it is possible that investors do not simply increase their allocation toward the asset with the highest
expected return and instead choose the asset with the highest expected return per unit of risk. We investigated this possibility by normalizing the future returns either by the ex-ante expected own-market volatility (\(\hat{\sigma}_{jj,t+1}\)) or by the conditional covariance with returns on U.K. stocks (\(\hat{\sigma}_{juk,t+1}\)), both obtained from the bivariate GARCH model, eq. (2). The results, reported in panels B and C of table 4, do not change very much, suggesting that the evidence on market timing is robust in the presence of time-varying risk.

C. Directional Tests

We next conducted a Merton-style market-timing regression based on indicator functions (taking the values unity or zero) for the sign of future returns. Let \(I_{\{\rho_{jt+1} \geq 0\}}\) be an indicator function for the event that future realized excess returns in region \(j\) relative to the world market average is positive or zero, while \(I_{\{\rho_{jt+1} < 0\}}\) is an indicator for the situation where future excess returns are negative. We estimated regressions

\[
\Delta \omega_{jt} = \beta_{1j} I_{\{\rho_{jt+1} \geq 0\}} + \beta_{2j} I_{\{\rho_{jt+1} < 0\}} + \varepsilon_{jt}. \tag{16}
\]

An unconditional measure of market-timing skills, proposed in this context by Graham and Harvey (1996), is whether \(\beta_{1j} > 0\), in which case the asset allocation to markets with positive future excess returns is increased and \(\beta_{1j} < 0\), in which case the allocation to markets with negative future excess returns is decreased. Panel A of table 5 shows that over 90% of all funds generated positive estimates of \(\beta_{1j}\) for Japan, Europe, and Asia; again the exception was North America, for which only 8% of funds obtained a positive estimate of \(\beta_{1j}\). Likewise, these unconditional regressions suggest that the funds successfully timed periods with negative excess returns, the proportion of negative coefficient estimates of \(\beta_{2j}\) ranging from 65 to 99%. These regressions have to be interpreted with considerable caution, however. For instance, the large percentage of funds generating a negative estimate of \(\beta_{2j}\) for North America is likely to reflect the long-run strategic asset-allocation decision of the funds to pull out of North America. This is different from tactical asset-allocation skills, as reflected in the ability to successfully switch in and out of markets in the short run according to the anticipated sign of future returns. A test of the tactical asset allocation skills, based on the independence between the sign of the portfolio weight change and the sign of future returns, was proposed by Henriksson and Merton (1981) and generalized to account for sampling variation in the estimated ‘hit rate’ by Pesaran and Timmermann (1992). We report the outcome of this test in panel B of table 5. When applied to the four regions, we find only very weak evidence of market-timing skills. Only for Europe did more than 5% of the funds generate a positive and significant value for this test statistic.
Equation (15) is also subject to the criticism that any market-timing skills reflected in the funds’ portfolio weight changes might simply reflect publicly available information. To see if the funds possessed market-timing skills over and above that contained in public information, we follow Graham and Harvey (1996) and perform conditional tests by regressing the current portfolio weight change on indicators for the sign of the unanticipated future return component,

\[ r_{jt+1}^{u} = r_{jt+1} - r_{jt+1}^{e} \]

as well as the anticipated part, \( r_{jt+1}^{e} \) (based on the earlier regression of regional returns on the lagged instruments, \( Z_t \)).

\[
\begin{align*}
\Delta \omega_{jt} &= \beta_{1j} I\{r_{jt+1}^{u} \geq 0\} + \beta_{2j} I\{r_{jt+1}^{u} < 0\} + \beta_{3j} I\{r_{jt+1}^{e} \geq 0\} + \epsilon_{jt}. \\
&= \beta_{1j} I_{\{r_{jt+1}^{u} \geq 0\}} + \beta_{2j} I_{\{r_{jt+1}^{u} < 0\}} + \beta_{3j} I_{\{r_{jt+1}^{e} \geq 0\}} + \epsilon_{jt}
\end{align*}
\]

If funds can predict the part of future differential returns unaccounted for by current public information (Graham and Harvey call this “extra-market-timing ability”), \( \beta_{1j} \) should be positive and \( \beta_{2j} \) should be negative.

### TABLE 5 Market Timing Skills in Up and Down Markets

<table>
<thead>
<tr>
<th></th>
<th>Japan</th>
<th>North America</th>
<th>Europe</th>
<th>Asia-Pacific</th>
</tr>
</thead>
<tbody>
<tr>
<td>A: ( \Delta \omega_{jt} = \beta_{1j} I_{{r_{jt+1}^{u} \geq 0}} + \beta_{2j} I_{{r_{jt+1}^{u} &lt; 0}} + \epsilon_{jt} )</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Median ( \hat{\beta}_{1j} )</td>
<td>0.0029</td>
<td>-0.0111</td>
<td>0.0031</td>
<td>0.0010</td>
</tr>
<tr>
<td>% of regressions with ( \hat{\beta}_{1j} &gt; 0 )</td>
<td>99.60</td>
<td>7.69</td>
<td>98.38</td>
<td>91.50</td>
</tr>
<tr>
<td>% of regressions with ( \hat{\beta}_{1j} &gt; 2 )</td>
<td>9.31</td>
<td>0.00</td>
<td>2.83</td>
<td>0.81</td>
</tr>
<tr>
<td>Median ( \hat{\beta}_{2j} )</td>
<td>-0.0023</td>
<td>-0.0222</td>
<td>-0.0011</td>
<td>-0.0005</td>
</tr>
<tr>
<td>% of regressions with ( \hat{\beta}_{2j} &lt; 0 )</td>
<td>98.79</td>
<td>93.93</td>
<td>80.57</td>
<td>64.77</td>
</tr>
<tr>
<td>% of regressions with ( \hat{\beta}_{2j} &lt; -2 )</td>
<td>2.02</td>
<td>9.31</td>
<td>0.40</td>
<td>0.00</td>
</tr>
</tbody>
</table>

### B: Henriksson-Merton Tests of Market Timing: Excess Returns

| % of funds with positive market timing test | 95.1 | 63.6 | 82.2 | 79.3 |
| % of funds with positive and significant test | 3.2 | 0.0 | 9.3 | 4.9 |

### C: Henriksson-Merton Tests of Market Timing: Unexpected Excess Returns

| % of funds with positive market timing test | 96.4 | 63.6 | 71.3 | 88.3 |
| % of funds with positive and significant test | 2.0 | 0.0 | 4.0 | 2.0 |

**Note.**—Panel A tests whether funds increased their portfolio weights (\( \Delta \omega_{jt} \)) in anticipation of a positive sign for next period’s excess return in a given region, \( j \), relative to the global average (\( r_{jt+1}^{e} \)). The panel also tests whether the funds had market-timing skills in down markets. \( I_{\{r_{jt+1}^{u} \geq 0\}} \) is an indicator function that takes a value of unity whenever the excess return in period \( t+1 \) is nonnegative and otherwise is zero. \( I_{\{r_{jt+1}^{u} < 0\}} \) takes a value of unity when \( r_{jt+1}^{u} \) is negative. Market-timing skills should show up as a positive value of \( \hat{\beta}_{1j} \) and a negative value of \( \hat{\beta}_{2j} \). The Henriksson-Merton (1981) tests (panels B and C) consider the null hypothesis that the sign of \( \Delta \omega_{jt} \) and \( r_{jt+1}^{e} \) are independently distributed. A positive and significant value of this test again indicates market timing skills. A 5% critical value was assumed throughout the table to assess statistical significance. The sample covers 247 U.K. pension funds over the period 1991:1–97:12.

13. We do not include a fourth indicator \( I\{r_{jt+1}^{e} < 0\} \), since in our application the pair of indicator functions \( I\{r_{jt+1}^{u} \geq 0\} \) and \( I\{r_{jt+1}^{e} < 0\} \) always sum to unity. Adding both \( I\{r_{jt+1}^{u} \geq 0\} \) and \( I\{r_{jt+1}^{e} < 0\} \) would induce perfect collinearity.
Table 6 shows very little evidence of extra-market-timing skills. While 80 and 92% of the funds generated positive estimates of $b_1$ for Japan and Asia-Pacific, only 0 and 2% of the funds did so for North America and Europe, respectively. Even weaker evidence emerges for the market-timing skills in down markets. Here, there is evidence of market-timing skills only in North America (95%) and negative evidence for Japan (15%), Europe (2%), and Asia (5%). Furthermore, some of the market-timing ability shown in Table 5 appears to reflect publicly available information, as evidenced by the many positive estimates of $b_3$ for Japan and Europe.

We also applied the Henriksson-Merton test to the relationship between the sign of the portfolio weight change and the unexpected future excess return. Compared with the outcome using total future excess returns, the results, as shown in panel C of Table 5, are even weaker. Only 2, 0, 4, and 2% of the funds generated a significant value of this market-timing test in the four regional markets.

D. Overall Measures of Market Timing

As a means of providing an overall summary measure of market-timing skills, we tested whether the funds correctly increase their portfolio weights the most for the region whose return next period is highest or, conversely, decrease their weights the most for the region with the smallest future return. We conducted this test using a simple $\chi^2$-test.
based on the diagonal cells in the $4 \times 4$ contingency table matching realized returns, $r_{jt+1}$, against weight changes, $\Delta \omega_{jt}$, in each of the four regions. We found that, using a 5% critical level, no fund showed any ability to consistently anticipate the market with the highest return, while only 1 out of 247 funds seemed able to anticipate which market would pay the lowest return.

Our evidence so far suggests that genuine market-timing skills are very weak. However, it also raises the possibility that U.K. pension funds may simply have followed the predictions from standard models of expected returns in revising their portfolio weights. To measure the total returns from extra-market-timing activities, for each region, we compute the return from that part of the portfolio weight which is orthogonal to time-varying moments, $\hat{\omega}_{ijt}^\mu = \omega_{ijt} - \hat{\omega}_{ijt}$, where $\hat{\omega}_{ijt}$ is the projection of $\omega_{ijt}$ on the conditional mean, variance, and covariance from eq. (2), rescaled to sum to unity. For each fund ($i$), the $\hat{\omega}_{ijt}^\mu$ sum to zero (across region $j$), so these weights represent a zero-investment portfolio. Summing across regions gives a measure of the total return to the zero-investment portfolio that tracks extra-market-timing skills:

$$\sum_{j=1}^{4} \omega_{ijt}^\mu r_{jt}. \quad (18)$$
The mean of the time-series average of this measure is $-0.16\%$ per annum when the portfolio weights are projected on expected returns, variances and covariances. Figure 4 provides a histogram of the statistic, demonstrating that there are two clusters of funds. The vast majority of funds belong to the cluster with a mean return from extra-market-timing of around $-0.25\%$ per year. A smaller cluster of funds is centered around a mean returns of $0.25\%$ per year. Only 29 out of 247 or $11\%$ of the funds generated positive mean returns from extra-market-timing. None of these time-series means was individually statistically significant, however.

V. Conclusion

Foreign investors’ market-timing activity has long been the subject of speculation. Reflecting on the large movements in international capital flows that occurred in the early 1990s, Lewis (1998) concludes that investors do not appear to follow passive buy-and-hold strategies in foreign markets. She conjectures that “domestic investors may be trying to follow market-timing strategies” (p. 27). However, little has previously been known about the factors influencing investors’ market timing and strategic asset-allocation decisions in international equity markets.

Several new insights into institutional investors’ behavior and performance in foreign equity markets have resulted from this study, chief of which is our finding that portfolio weights are highly correlated with time-varying expected returns, volatilities, and conditional covariances with global equity returns.

We decomposed the investors’ market-timing activity into two parts: that due to time-varying moments and that due to extra-market timing. The decision by U.K. pension funds to withdraw from the North American market and increase their allocation toward Europe appears to partially reflect the time series of expected returns in these markets in excess of expected returns in other foreign markets. Since the ex post realized returns in the North American market were very high during the sample, a Bayesian learning model of the kind advanced by Brennan and Cao (1997) cannot be used to explain this strategy.

While we find weak evidence in support of international market-timing skills based on standard, unconditional performance regressions, this evidence becomes much weaker in tests that account for a time-varying global investment opportunity set. Our estimates suggest that, when we orthogonalize portfolio weight movements with respect to predictable time-varying moments, the average extra-market-timing performance was $-0.2\%$ per annum.

14. When the portfolio weights were projected on expected returns and variances, leaving out covariances with global returns, the average of the market timing statistic was $-0.20$. 
References


