Information versus Investment

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Abstract

Firms both make long term investments and reveal information about performance. These activities serve crucial roles in the economy and capital markets, yet they are in direct conflict in the presence of realistic managerial incentives to smooth reported performance. To gauge the quantitative importance of this tradeoff, we estimate a dynamic model that captures the tradeoff between investment efficiency and information accuracy. The model matches a range of observable moments constructed from data on firm investment and periods of detected misreporting by firms. Managers in our model distort reported profits on average by 3% of sales. Counterfactual analysis reveals that eliminating this misreporting through disclosure regulation is possible, but doing so incentivizes managers to distort real investment. The result would be around 1% lower firm value on average, reflecting a quantitatively meaningfully tradeoff.

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1. Introduction

Shareholders rely on firm managers to carry out two distinct tasks: making long-term investment choices and disclosing information about firm performance. Both tasks matter. Firm investment ensures the long-term growth of the firm, while accurate disclosure of financial information allows for the efficient pricing of assets, which is essential for the health and transparency of capital markets overall. Unfortunately, in an incomplete contracting environment, managers’ incentives need not be set to perform these two tasks optimally, so it is possible to observe a trade-off between the accurate disclosure of information and the efficiency of investment choices. A large literature on capital misallocation in economics examines the negative impact of distortions or frictions that reduce the efficiency of investment. We contribute to this literature by quantifying the real effects of frictions that induce firms to substitute between making efficient investment choices and revealing accurate information. In other words, we examine whether there is in fact a meaningful tradeoff between the efficiency of firm investment and the quality of information disclosure.

This question is difficult because information frictions are notoriously hard to measure, as we almost never observe the information that has been concealed, only the ongoing equilibrium with information barriers. To overcome this hurdle, we turn to the arena of earnings misreporting, which is a natural laboratory to examine a question involving information. Data on earnings announcements, realizations, and restatements are widely available. Moreover, while instances of fraudulent disclosure are infrequent, they exist, so we can observe a snapshot of investment decisions surrounding deliberate information manipulation. Of course, not all fraudulent disclosure is detected, with the result that quantifying the economic magnitude of the relevant information frictions requires imposing some structure on the data.

Therefore, we use these data to estimate a dynamic model of earnings reporting and real intangible investment, where we focus on intangible instead of fixed investment because accounting rules imply expenditures on intangibles have much larger impact on than fixed
investment expenditures. The basic idea is simple: managers facing short-term incentives to distort the information available to investors can do so either through misreporting their financial statements, through distortions of their investment choices, or through both actions at once. The implication is that if disclosure regulation causes the cost of one tool for manipulation to change, then in equilibrium use of the other tool will be affected. To reflect this notion, in the model, managers have incentives to manipulate both information about earnings and intangible investment, but they also face costs if they are caught manipulating.

The model matches a wide array of data moments related to both real investment outcomes and accounting restatements. Moreover, in the estimated model, managers choose reporting bias equal to around 3% of sales, conditional upon restatement. When we counterfactually make information manipulation prohibitively costly, managers optimally manipulate earnings more via adjustments to intangible investment. On average, firm value drops by just under 1%, a nontrivial real cost.

The intuition behind these results requires a more complete description of the model, which features conflicting managerial incentives. On the one hand, managers have long-term incentives that are aligned with shareholder incentives and that are delivered by stock compensation. This part of managers’ compensation package implies that they benefit when they make efficient investment choices and are hurt when they do not. On the other hand, incentive alignment between managers and shareholders is incomplete, as pressure to beat last period’s earnings gives managers short-term incentives to manipulate information either by lying about earnings or by cutting investment expenditures. However, these short-term incentives are tempered because the manager can with some probability get caught and face punishment, which is the notion of disclosure regulation in the model.

With this incentive structure in place, managers then choose both long-term investment and short-term earnings manipulation to maximize their utility over an infinite horizon. They face a stochastic, decreasing returns production function that transforms intangible investment into sales, with the stochastic portion of this technology exhibiting persistence. They also face
an exogenous, privately observed, transitory shock to earnings, which is non-fundamental in
the sense that it has no effect on actual cash flows, while at the same time affecting reported
earnings. Because we assume that investors use an information set that is more restricted than
the manager’s, investors cannot distinguish true from reported earnings and thus compensate
the manager based on the reported earnings. Therefore, managers misreport earnings and also
opportunistically either cut or overinvest in intangible capital at suboptimal times. The result
is less accurate information provision to the public and intertemporal capital misallocation
that produces an efficiency loss in real terms.

In the face of the incentives described above, a manager’s choices deviate meaningfully from
a value-maximizing benchmark. In particular, managers facing negative transitory shocks to
earnings often choose lower levels of intangible investment in order to boost profits and deliver
earnings growth. In contrast, managers facing high or positive transitory shocks will usually
boost their investment, thus smoothing earnings today and providing a more feasible target
for tomorrow. The result is high sensitivity of investment to a transitory, non-fundamental
shock that a forward-looking, value-maximizing firm would ignore entirely. Moreover, because
managers can manipulate information both by misreporting and by investing suboptimally,
investment policies in the model depend crucially upon disclosure regulation, which governs
the manager’s flexibility in biasing or misreporting information.

Our results would have been hard to obtain in a reduced form setting. Although managers
can be caught misstating earnings, and although these episodes result in earnings restate-
ments, manipulation or biases in reported earnings likely go unobserved most of the time.
Moreover, the mechanisms whereby earnings manipulation spills over into real outcomes are
also unobservable. Questions that are couched in terms of unobservables are prime candidates
for structural estimation. For example, Zakolyukina (forthcoming) also takes a structural
approach to the estimation of the likelihood of misreporting. We build upon this work by
examining not only the probability of manipulation, but also the spillover onto real firm
decisions.
The general notion that there is a tradeoff between information and investment is grounded in the survey evidence in Graham, Harvey, and Rajgopal (2005) that managers rely on both misreporting and investment distortions to manipulate earnings, with many expressing a willingness to cut intangible investment such as R&D and advertising expenditures in order to hit an earnings target. In addition, even a cursory pass at the data provides evidence consistent with the survey’s suggestions. Figure 1 plots the dynamics of intangible investment and earnings reporting bias around periods in which firms are publicly forced to revise their earnings downward, based on a sample of data that we discuss further below. Investment is around 2.5% lower in periods in which firms misreport their earnings, while earnings are biased upward at the same time. The concurrence of a dip in investment with a misreporting event is consistent with the idea that firms do indeed rely jointly on both investment and reporting tools for manipulation. The natural implication is that reduced flexibility in misreporting can in theory result in managers’ reliance on value destroying investment distortions, which we term real manipulation.

This tradeoff matters because it imposes an equilibrium constraint on policy. For example, disclosure regulation, such as the Sarbanes-Oxley Act (SOX), has been criticized for forcing firms to substitute real earnings manipulation for manipulation based on the misreporting of accounting accruals (Cohen, Dey, and Lys 2008). More generally, because compensation packages with short-term incentives prompt managers to manipulate, and because these packages are pervasive (Edmans, Gabaix, and Jenter 2017), increasing information accuracy can lower real efficiency. Thus, quantifying the extent of this substitution is clearly of interest to policymakers and corporate boards.

These results are also of interest to macroeconomists, given the large literature linking endogenous growth of the economy as a whole to sustained intangible investments at the firm level. As such, distortions to long-term or intangible investments through earnings pressure may have important macroeconomic consequences, as emphasized recently by Terry (2015). Moreover, the link between intangible investment and earnings manipulation seems intuitive,
as intangible investments like R&D and advertising are expensed rather than capitalized and subsequently depreciated. Therefore, these investments provide an immediate impact on current-period earnings figures, so they are a natural tool for manipulation.

Our project links to two distinct literatures. The first is the accounting literature that examines earnings management, as managers in our model engage in two types of management: accruals manipulation, which occurs through earnings misreporting, and real manipulation, which occurs through opportunistic changes to long-term investment. As such, this paper contributes to the empirical literatures on both accrual-based and real earnings management.

Empirical patterns consistent with accruals and real manipulation have been documented in reduced-form studies in accounting for decades. This literature traditionally measures both accrual-based and real earnings management using residuals from linear regressions. For example, accrual-based earnings management is measured via discretionary accruals models, which are regressions of total accruals on variables correlated with theoretical normal accruals (e.g., Jones 1991; Dechow, Sloan, and Sweeney 1995; Kothari, Leone, and Wasley 2005). Similarly, discretionary R&D expenditures are residuals of regressions with R&D as a dependent variable (e.g., Roychowdhury 2006; Cohen et al. 2008; Zang 2011). Using these measures, the literature has documented substitution between these regression-based measures of accrual-based and real earnings management (e.g., Cohen et al. 2008; Cohen and Zarowin 2010; Zang 2011).

We advance this literature by substituting an economic model for statistical models of manipulation and R&D. The advantage of this approach is twofold. First, we can quantify the real-accruals manipulation substitution slope. This step is both a quantitative and qualitative advance beyond the reduced-form evidence that predates ours, as the notion of the slope of a tradeoff is difficult to formulate in a regression framework. Moreover, we address the call in Leuz and Wysocki (2016) for more research on the real effects of disclosure regulation and its aggregate impact on the economy.¹

¹As we model explicit incentives for manipulation, our paper also touches on the theoretical and empirical literature on moral hazard problems that can arise from performance manipulation. See, for example, Lambert
Second, we contribute to the large literature in finance and macroeconomics that studies distortions to real investment decisions. Here, our contribution is a demonstration that distortions caused by earnings pressures and information manipulation constitute a distinct and quantitatively important friction alongside long-studied forces such as financial frictions, adjustment costs, or agency frictions, as in Cooper and Haltiwanger (2006), Hennessy and Whited (2007), and Nikolov and Whited (2014). We enter this picture by using transparent structural estimation to determine the quantitative relevance of the trade-off between information revelation and investment efficiency.

Our model builds on several features of models in this literature. For example, firms in the model are subject to exogenous shocks to their productivity or profitability as in Hopenhayn (1992). Simultaneously, managers choose intangible investment that leads to innovation and endogenous growth from new ideas. At its core, the model features growth at the micro level that shares the same source—innovation—as models of macro-level endogenous growth (Romer 1990; Aghion and Howitt 1992). Because idiosyncratic shocks differentiate firms and drive their innovation decisions, the firm-level environment or heterogeneity is richer than in many baseline models of endogenous growth, although lumpy innovation arrivals and entry/exit dynamics are absent.

Two papers are particularly closely related to ours. The first is Terry (2015), which, like our work, examines the effects of information manipulation on R&D. However, our work is distinct in several ways. While Terry (2015) uses a general equilibrium framework to analyze economy-wide impacts of short-term incentives, we use a more flexible partial equilibrium framework that allows us to make richer firm value statements. More importantly, this flexibility also allows us to examine cross-sectional heterogeneity in the effects of manipulation, as well as the large structural breaks in information disclosure rules stemming from the Sarbanes-Oxley Act. Because of this model flexibility, we also employ a richer misreporting environment, allowing us to endogenously target micro data on earnings restatements to

identify the model parameters related to manipulation. In contrast, the misreporting structure of Terry (2015), which focuses on macroeconomic effects instead of microeconomic policy implications, is more stylized in nature.

The second closely related paper is Benmelech, Kandel, and Veronesi (2010), which explores how stock-based compensation induces managers to conceal information and choose suboptimal investment policies. While their model shares several important tradeoffs with ours, their analysis is theoretical. We extend this line of research by attempting to quantify the empirical relevance of the frictions that force important interactions between investment efficiency and information disclosure.

The remainder of the paper is organized as follows. Section 2 develops our model and analyzes optimal policies. Section 3 describes our data and provides summary statistics. Section 4 outlines our estimation strategy. Section 5 presents estimation results and our counterfactuals. Section 6 concludes.

2. Model

Time is discrete and the horizon is infinite. There is a unit mass of infinitely lived firms, each of which is run by a manager who receives both equity compensation and faces short-term pressure to sustain last period’s earnings. He chooses intangible investment, as well as potential earnings misreporting to maximize his own utility.

2.1 Firms and Fundamentals

The firm’s revenue net of flexible inputs, $Y$, is the product of endogenous quality, $Q$, and exogenous productivity, $\nu_y$, which follows an $AR(1)$ process in logs:

$$\log \nu_y' = \rho_y \log \nu_y + \eta_y', \quad \eta_y' \sim N(0, \sigma_y^2).$$  \hfill (1)
Here, a prime indicates a variable in the subsequent period, and $|\rho_y| < 1$. Consistent with much of the endogenous growth literature (Romer 1990), the production function $Y = \nu_y Q$ exhibits increasing returns in the sum of endogenous quality, $Q$, and exogenous quality, $\nu_y$. The manager can choose expenditures in intangible capital or R&D, denoted as $W$, which drives growth in endogenous productivity $Q$ according to:

$$Q' - Q = \Delta Q' = \xi W^\gamma Q^{1-\gamma}, \quad 0 < \gamma < 1.$$  \hspace{1cm} (2)

The parameter $\xi$ is a multiplicative productivity shifting parameter. For simplicity, we assume that $Q$ does not depreciate and there are no adjustment costs for intangible investment. These assumptions are innocuous, as none of our eventual model predictions depend on the variable $Q$.

This investment technology exhibits decreasing returns, given by $\gamma$, and it implies that the growth rate in endogenous productivity is identically given by:

$$g \equiv \frac{\Delta Q'}{Q} = \xi \left(\frac{W}{Q}\right)^\gamma.$$  

Distributions to shareholders, $D$, are given by output minus R&D:

$$D \equiv Y - p_w W,$$  \hspace{1cm} (3)

in which $p_w$ is the price of R&D relative to output. Because we have no depreciated capital expenditures in the model, from an accounting perspective, $Y - p_w W$ can be thought of as intrinsic earnings that ultimately convert to shareholder cash flows. We abstract from physical capital accumulation for two reasons. First, because investment in property, plant, and equipment is not immediately expensed, this type of investment only has an impact on earnings when it is depreciated, so the ex ante likelihood of a large impact on earnings management is small. Second, we want to maintain model simplicity and tractability.
2.2 Reporting and Manipulation

In each period, the firm must report its earnings, $\Pi$, to investors. We allow for observed earnings to deviate from intrinsic earnings, $Y - p_w W$, in two ways. First, we specify an accounting shock, $\nu_\pi$ that drives non-fundamental exogenous variation in earnings $\Pi$, with

$$\nu_\pi \sim N(0, \sigma^2_\pi).$$

(4)

This shock has no actual cash flow consequences and simply reflects deficiencies in accounting standards related to accurate estimation of intrinsic cash flows. Below, we refer to the shock, $\nu_\pi$, as a non-fundamental shock or profit shock.

Second, the manager can manipulate earnings by introducing bias into the book value of the firm because earnings represent the first difference of book value. As such, the manager enters the current period with an inherited bias in book value given by $B_{-1}$. He then chooses a new level of bias, $B$, to obtain a net distortion, $B - B_{-1}$, to reported earnings. These two extra components of earnings imply that

$$\Pi \equiv Y - p_w W + \nu_\pi Q + B - B_{-1}.$$  (5)

This specification allows for the mechanical partial reversal of accruals-based manipulation because the manager can always compensate for any reversal of bad accruals by manipulating even more with an appropriate choice of $B$.

If the new choice of bias, $B$, is nonzero, then the manager faces a constant probability, $\lambda$, of discovery.\(^2\) This model feature realistically implies that a manager can go for some time without getting caught. In addition, he can also reverse the manipulation in those periods in which he does not get caught and thus remain forever undetected for that specific episode of

\(^2\)While intuition would suggest that the probability of detection ought to depend on the size of the bias, the rarity of restatements does not allow us to identify the relation between bias size and detection probability.
manipulation. If he is discovered, he must pay a private cost of

\[ MC(B, Q) = \left( \kappa_f + \kappa_q \left( \frac{B}{Q} \right)^2 \right) Q, \quad \kappa_f, \kappa_q \geq 0. \]  

(6)

In principle, such costs could arise either outside the firm from investor pressures or litigation risk. Alternatively, they could arise inside the firm as a part of a sophisticated manager compensation contract. In addition, such costs could represent real disruptions and resource losses for the firm itself (e.g., litigation risk) or purely non-pecuniary internal costs for the manager (e.g., career or reputational concerns). In our counterfactuals below, we want to isolate the effects of these costs on managerial actions, and we want to avoid a purely mechanical impact of the costs themselves on the implied changes in firm value. Therefore, we conservatively assume that all of the smoothing and misreporting incentives reflected in (6) are purely non-pecuniary and internal to the manager. Finally, we assume that upon discovery and after payment of the private cost, \( MC(B, Q) \), bias is unwound.

2.3 Managers’ Incentives

Managers are risk neutral, and their compensation contracts have two components. The first is a fixed fraction, \( \theta_d > 0 \), of the outstanding equity of the firm, so the manager receives the same fraction, \( \theta_d \), of the distributions to shareholders. The second component is the short-term pressure to sustain last period’s earnings, \( \theta_f \geq 0 \). We assume that each period the manager is incentivized to report earnings at least as high as last period’s earnings, denoted as \( \Pi_{-1} \). Thus, each period the manager receives a cash flow of \( D_M \), which is given by:

\[ D_M \equiv \theta_d D + \theta_f 1 \{ \Pi \geq \Pi_{-1} \}. \]  

(7)

This payoff omits fixed compensation because the manager’s risk neutrality renders such compensation irrelevant for the manager’s choice of policies. The two components of compensation that we model have important implications for the manager’s actions. The stock
component aligns the managers’ incentives with those of long-term shareholders, while the short-term earnings growth component gives the manager an incentive to report current period’s earnings at least as high as last period’s earnings. While we model the incentives to improve over last period’s earnings for simplicity, any compensation scheme that has jumps in the measures of firm performance, such as the stock price or earnings, would provide similar incentives. Performance-based equity grants, options-based compensation, and bonus plans serve as examples.

We motivate this compensation scheme in large part by the survey of CEO compensation by Frydman and Jenter (2010), which documents that most CEO compensation packages contain salary, bonuses, payouts from long-term incentives plans, and restricted option and stock grants. Performance-based equity grants have been increasing since the mid-1990s (Bettis, Bizjak, Coles, and Kalpathy 2010) and have outpaced options as the most popular form of equity compensation after 2004 (Edmans et al. 2017). Similar to bonus plans, these performance-based equity grants often have a discrete jump at the lower performance threshold and an “incentive zone” (Bettis, Bizjak, Coles, and Kalpathy 2018). These plans are often very complex and, for instance for performance shares, can have linear or non-linear mapping from performance to the number of securities granted in the incentive zone. They are also often based on many performance metrics (e.g., Gerakos, Ittner, and Larcker 2007; Bettis et al. 2010, 2018). Accounting-based performance metrics are used more frequently than stock-based metrics, with earnings-based metrics being the most common accounting measure (Edmans et al. 2017). We focus on the discrete jump in compensation and abstract away from the performance-payoff mapping in the incentive zone. Besides the complexity of performance-based equity compensation contracts, another reason to consider only discrete jumps is the large literature on “meeting or beating” earnings targets. This literature shows that reported earnings tend to exceed three thresholds: avoiding losses, sustaining recent earnings, and meeting analysts’ expectations (e.g., Burgstahler and Dichev 1997; Degeorge, Patel, and Zeckhauser 1999). For these reasons, we focus on last period’s earnings as a performance
As in Nikolov and Whited (2014) and Glover and Levine (2017), we remain silent on the optimality of these incentives. Instead, we seek to quantify empirically the trade-off between information and investment in the face of incentives that are widely observed but that do not necessarily induce behavior that maximizes shareholder value. This strategy is sensible given the evidence in Dittmann and Maug (2007) that standard principal-agent models cannot rationalize observed executive compensation contracts. Alternatively, another reasonable view of this compensation policy is that it is a reduced-form description of a contracting outcome that allows for equilibrium self-interested behavior on the part of the agent, as in Zhu (2013). One final alternative interpretation of our contracting specification is that the contracting environment is incomplete and that the contract we specify is optimal, given an agency issue that is both outside the model and that we do not observe. The incompleteness of the contracting environment would then imply that the misbehavior that we model cannot be contained via contracts.

2.4 Managers’ Dynamic Optimization Problem

We now describe the manager’s dynamic optimization problem. He faces a state vector at any time of \((\nu_y, \nu_\pi, \Pi_{-1}, B_{-1}, Q)\), and he discounts cash flows at a rate \(r\). He optimally chooses R&D, \(W\), and new gross bias, \(B\). Given that the manager wants to maximize the expected discounted value of his compensation, the manager’s private value function is given by \(V_M\), as follows:
subject to the constraints and definitions given in (1)–(7). The first line in curly brackets in (8) is the value to the manager if he chooses not to engage in book-value manipulation. The second line represents the case in which he chooses to manipulate but does not get caught. The third line represents the case in which he does get caught.

While (8) gives lifetime managerial utility, it does not represent the fundamental value of the firm, which we denote as $V_F$, and which is simply the expected present value of distributions to shareholders. On the basis of the manager’s privately optimal policies $B^*$ and $W^*$, the fundamental value of the firm $V_F$ is thus given by

$$V_F(\nu_y, \nu_\pi, \Pi_{-1}, B_{-1}, Q) = \max_{W,B} \left\{ \begin{array}{l} \mathbb{I}(B = 0) \left( D_M + \frac{1}{1+r} \mathbb{E}V_M(\nu_y', \nu_\pi', \Pi, 0, Q') \right) \\ + \\
\mathbb{I}(B \neq 0)(1 - \lambda) \left( D_M + \frac{1}{1+r} \mathbb{E}V_M(\nu_y', \nu_\pi', \Pi, B, Q') \right) \\ + \\
\mathbb{I}(B \neq 0) \lambda \left( D_M|B=0 - MC(B, Q) + \frac{1}{1+r} \mathbb{E}V_M(\nu_y', \nu_\pi', \Pi|B=0, 0, Q') \right) \right\} , \tag{8} \right.$$
by endogenous productivity, $Q$, as follows:

$$ y \equiv \frac{Y}{Q} = \nu_y, \quad d \equiv \frac{D}{Q} = y - p_w w, \quad w \equiv \frac{W}{Q}, \quad g = \xi w^\gamma. $$

Earnings also naturally scale linearly with $Q$, so scaled earnings are given by:

$$ \pi \equiv \frac{\Pi}{Q} = y - p_w w + \nu_\pi + b - b_{-1}, \quad b \equiv \frac{B}{Q}, \quad b_{-1} \equiv \frac{B_{-1}}{Q}. $$

Similarly, normalized by endogenous productivity, $Q$, manager incentives are given by

$$ d_m \equiv \frac{D_M}{Q} = \theta d + \theta f I \{ \pi \geq \pi_{-1} \}. $$

The manager’s value function (8) is homogeneous in $Q$, so we can write

$$ V_M(\nu_y, \nu_{\pi}, \Pi_{-1}, B_{-1}, Q) = Q v_m(\nu_y, \nu_{\pi}, \pi_{-1}, b_{-1}), $$

where the normalized manager value function is given by

$$ v_m(\nu_y, \nu_{\pi}, \pi_{-1}, b_{-1}) = \max_{w, b} \left\{ \begin{array}{c}
\mathbb{I}(b = 0) \left( d_m + \frac{1 + g(w)}{1 + r} \mathbb{E} v_m(\nu_y', \nu_{\pi}', \frac{\pi}{1 + g(w)}, 0) \right) \\
\mathbb{I}(b \neq 0) (1 - \lambda) \left( d_m + \frac{1 + g(w)}{1 + r} \mathbb{E} v_m(\nu_y', \nu_{\pi}', \frac{\pi}{1 + g(w)}, \frac{b}{1 + g(w)}) \right) \\
\mathbb{I}(b \neq 0) \lambda \left( d_m \big|_{b=0} - mc(b) + \frac{1 + g(w)}{1 + r} \mathbb{E} v_m(\nu_y', \nu_{\pi}', \frac{\pi}{1 + g(w)}, b = 0, 0) \right) \end{array} \right\} $$

(10)
subject to the following constraints and processes:

\[ y = \nu_y, \quad \log \nu_y = \rho_y \log \nu_{y,-1} + \eta_y, \quad \eta_y \sim N(0, \sigma_y^2) \]

\[ d = y - p_w w \]

\[ \nu_\pi \sim N(0, \sigma_\pi^2) \]

\[ \pi = y - p_w w + \nu_\pi + b - b_{-1} \]

\[ d_m = \theta_d d + \theta_f 1 \{ \pi \geq \pi_{-1} \} \]

\[ mc(b) = MC(b, 1) \]

\[ g(w) = \xi w^\gamma \]

An equivalent scaled concept for fundamental firm value \( v_f \equiv \frac{V_F}{Q} \) exists, which is given by

\[
v_f(\nu_y, \nu_\pi, \pi_{-1}, b_{-1}) = \begin{cases} 
\mathbb{I}(b = 0) \left( d + \frac{1 + g(w)}{1 + r} \mathbb{E} v_f(\nu'_y, \nu'_\pi, \frac{\pi}{1 + g(w)}, 0) \right) \\
\mathbb{I}(b \neq 0) (1 - \lambda) \left( d + \frac{1 + g(w)}{1 + r} \mathbb{E} v_f(\nu'_y, \nu'_\pi, \frac{\pi}{1 + g(w)}, \frac{b}{1 + g(w)}) \right) \\
\mathbb{I}(b \neq 0) \lambda \left( d + \frac{1 + g(w)}{1 + r} \mathbb{E} v_f(\nu'_y, \nu'_\pi, \frac{\pi}{1 + g(w)} | b = 0, 0) \right)
\end{cases}
\]

(11)

Here, the fundamental firm value function is evaluated at the optimal policies \( b, w \) derived from the manager dynamic optimization, and the transitions and constraints are identical to those in the definition of \( v_m \).

Scaling implies that all of our lower case variables are measured in terms of dollars per quality unit. Because quality units are unobservable, our model has natural empirical predictions for the growth rates and ratios of observable variables, but not for the levels.
2.5 Model Solution Algorithm

To solve the model, which does not have a closed-form solution, we rely on standard numerical
dynamic programming techniques applied to the stationary (scaled) recursive formulation
in (10). Besides the usual challenge of solving a model with a high number of endogenous
policies and state variables, however, there is an additional complication introduced by the
non-stationarity of the underlying problem in this firm-level growth model. The solution is
sensitive to the discounting implied by the quality growth rate, \( g(w) \), which appears both
in the continuation values of (10) as well as in the endogenous state transitions. Because
a firm’s desired R&D level, \( w \), and hence its growth rate, \( g(w) \), depend crucially upon the
efficiency of R&D, as embodied in the parameter \( \xi \), the value of the parameter \( \xi \) matters a
great deal for the stability and nature of the implied numerical solution of the model. To
ensure a reasonable value for growth and a stable solution, we iterate on the value of R&D
efficiency \( \xi \) until one of the easily observed growth rates in the model matches its empirical
counterpart.

We implement the procedure as follows. First, given a vector of parameter values excluding
\( \xi \), we compute the average sales growth rate from the data, \( \hat{g}_{data} \). Next, we choose the value
of \( \xi \) in the model to satisfy the following equation:

\[
g_{y}^{sim}(\xi) = \hat{g}_{y}^{data},
\]

(12)
in which \( g_{y}^{sim}(\xi) \) is the average sales growth rate in the model. We solve (12) via bisection,
re-solving the model at different candidate values of \( \xi \) until (12) holds to a preset tolerance.
This algorithm for determining the value of \( \xi \), whose value depends both upon the empirical
sales growth rate as well as value of the other parameters in the model, works well in practice.
2.6 Revenue Recognition

The model contains one further parameter that does not enter into the managerial optimization problem but that does enter into the simulation of data from the model and is important for matching simulated with actual data moments. This parameter reflects accrual accounting, which is an important feature of earnings measurement and which is designed to provide a better indication of company’s performance or economic earnings than operating cash flows (FASB 1978).³

Accrual accounting induces a wedge between the measurements of earnings and operating cash flows, so accounting earnings do not generally correspond to cash inflows and outflows for the period. Moreover, because accruals are managers’ forecasts of future cash flows, these forecasts must reconcile with realized cash flows in the future (e.g., Allen, Larson, and Sloan 2013; Nikolaev 2016). This reconciliation property implies that we can view operating cash flows as a reshuffling of accounting earnings across adjacent periods. As such, we allow for a random portion of accounting earnings to be realized as cash flows in the periods immediately before or immediately after the current period. Although we allow for reshuffling in only one adjacent period, this idea is similar to the mechanism underlying the accrual quality measure in Dechow and Dichev (2002), who represent accounting earnings as the sum of past, present, and future cash flows that are recognized in the current period earnings, with an allowance for estimation errors.

To implement this principle, we first define a parameter \( \hat{p}_s \in (0, 1) \), which represents the probability of intertemporal cash flow reshuffling. Next, we draw a set of uniform shocks, \( \zeta_{it} \), \( \forall i, t \), where \( i \) indexes firms and \( t \) indexes time. We then initialize observed cash flows at time 1, which we denote \( \tilde{d}_{i,1} \), equal to the actual cash flow simulated directly from the model, that is, \( \tilde{d}_{i,1} \equiv y_{i,1} - p_w w_{i,1} \). Finally, iteratively progressing from \( t = 2, ..., T - 1 \) for each firm

³According to Statement of Financial Accounting Concepts No. 1, “Information about enterprise earnings based on accrual accounting generally provides a better indication of an enterprise’s present and continuing ability to generate favorable cash flows than information limited to the financial effects of cash receipts and payments.”
i, we update the observed cash-flow series by the following rules:

If \( \zeta_{it} < 0.5 \), set \( \tilde{d}_{it-1} = \tilde{d}_{it-1} + 2\hat{p}_s(0.5 - \zeta_{it}) \) and \( \tilde{d}_{it} = \tilde{d}_{it} - 2\hat{p}_s(0.5 - \zeta_{it}) \)

If \( \zeta_{it} > 0.5 \), set \( \tilde{d}_{it+1} = \tilde{d}_{it+1} + 2\hat{p}_s(\zeta_{it} - 0.5) \) and \( \tilde{d}_{it} = \tilde{d}_{it} - 2\hat{p}_s(\zeta_{it} - 0.5) \).

In words, this procedure randomly pushes forward some portion of today’s cash flows into tomorrow and yesterday, given the random mistiming or reshuffling shock, \( \zeta_{it} \), keeping the sum of cash flows over any medium-term horizon unchanged, where here the horizon is three years.

### 2.7 Optimal Policies

Each period, the manager chooses how much to invest and whether to bias her earnings report. Figure 2 plots her choices as a function of the persistent fundamental shock, \( \nu_y \) (left column) and the transitory profit shock \( \nu_\pi \) (right column). The top row plots the mean investment or R&D choices of the firm as a function of each shock, and bottom row plots the mean bias chosen by managers.

In the top left panel, we see an intuitive positive response of R&D investment to the fundamental shock because higher values of the persistent shock today indicate a higher average marginal product of R&D. Such a pattern and mechanism would also be present in a fully value maximizing model.

However, \( \theta_f > 0 \) in the estimated model implies the presence of managerial manipulation incentives, so managers also adjust R&D investment in response to the transitory profit shock, \( \nu_\pi \) (top right panel). This profit shock contains no information about the payoff to investment, and a value maximizing manager would ignore it. However, a low short-term transitory shock today on average causes managers with earnings growth incentives to cut intangible investment. Conversely, a high short-term profit shock creates higher profits today and a more difficult earnings benchmark tomorrow, so managers have an incentive to increase
R&D to dampen the realized increase in profits. The result is a positive relation between R&D on $\nu_\pi$ seen in Figure 2.

The manager’s choice of bias also responds to the fundamental and profit shocks. For example, in order to boost profits above lagged levels, managers with low levels of the fundamental shock choose a level of bias higher than the level chosen by managers with high levels of the fundamental shock (bottom left panel). As seen in the bottom right panel, the relation between bias and the profit shock is hump-shaped. For low realizations of the profit shock, the manager is unlikely to meet her target. Because the profit shock is transitory, she therefore chooses a lower bias level to bring down next period’s earnings target. By contrast, a manager with an intermediate level of the profit shock biases upwards by a great deal because this policy allows her to meet her current earnings threshold. Finally, a manager with a high level of the profit shock is likely to meet the earnings target regardless of the choice of bias, so she chooses to bias downwards to ensure that tomorrow’s earnings target is not too high.

The main message from Figure 2 is that managers choose to use both investment and bias as tools for profit manipulation, allowing for substitution between the two. Moreover, the responsiveness of investment to non-fundamental transitory shocks to profits implied by the estimated model implies substantial scope for misallocation and lost firm value.

3. Data

3.1 Sources

The data come from several sources. The financial data are from Compustat, and the data on executive compensation are from Equilar, which collects these data from annual proxy filings (DEF 14A). Its coverage is more than double the coverage of Compustat ExecuComp, whose universe is the S&P 1500. In contrast, Equilar covers virtually all public companies. The data on restatements are from Audit Analytics, where we use restatements that correct accounting errors as a measure of detected misstatements.
Data availability from the intersection of these three sources means that our sample spans sixteen years from 2000 to 2015 and includes firms incorporated in the United States and listed on the NYSE, Amex, or NASDAQ. For firms included in the sample, we require all variables used in the estimation to be non-missing. Because we need sufficient time-series variation in our data to identify some of our model parameters, we also require seven years of sales revenue data, where three years of these data must be consecutive. We further consider two samples of firms. The first sample excludes firms for which all SG&A expenses are missing or zero (SG&A sample), and the second sample excludes firms for which all R&D expenses are missing or zero (R&D sample). These restrictions retain firms for which the discretionary investment into SG&A or R&D decisions are relevant. For both samples, we further exclude firms in the financial and utilities sectors, which we define as Global Industry Classification Standard (GICS) sectors 40, 55, and 60. For the R&D sample, we also exclude transportation (GICS sector 2030) and food and staples retailing (GICS sector 3010). Table 1 provides definitions of all of our variables.

Although manipulation is chosen optimally by the manager in the model, not all restatements observed in the data correct intentional manipulation (Karpoff, Koester, Lee, and Martin 2017). As such, classifying restatements as intentional incurs some unavoidable discretion, and the choice of any particular definition of an intentional restatement reflects a trade-off between the number of restatements and the likelihood that these restatements correct intentional misstatements. We therefore adopt two definitions of an intentional misstatement.

The first definitions includes restatements of revenue recognition errors, where we identify revenue recognition restatements with the Audit Analytics data. Because all considered restatements are related to errors, our sample excludes retrospective revisions related to the application of SEC Staff Accounting Bulletin (SAB) No. 101 restatements. Thus, our sample includes only errors in SAB 101 implementation. Revenue recognition restatements elicit the largest negative market reaction relative to other types of errors (e.g., Palmrose, Richardson, and Scholz 2004; Scholz 2008). Moreover, the closely related model of intentional manipulation
in Zakolyukina (forthcoming) has more power to explain these types of errors relative to other types of errors such as expense recognition errors.

The second definition includes restatements classified as irregularities under three criteria. The first criterion is irregularity restatements as classified in Hennes, Leone, and Miller (2008). To create this group, we search all of Audit Analytics’ restatement disclosure narratives for the three criteria defined in this paper. The first is the presence of the derivative forms of the words “fraud” or “irregularity.” The second is SEC or Department of Justice formal or informal investigations. The third is discussion of independent investigations by an audit committee or a special committee. After automatic pre-screening for search terms, we read each relevant disclosure to make a final judgment about whether the particular disclosure satisfies the irregularity criteria.

The second criterion is restatements surrounded by events pointing to potential irregularities as specified in Appendix 2 in Cheffers, Usvyatsky, and Pakaluk (2014). For instance, these events include CEO or CFO dismissals due to internal investigations or suspected wrongdoing, auditor changes related to SEC inquiry or management unreliability, or the restated period overlapping with the violation period alleged by the Accounting and Auditing Enforcement Releases (AAERs) from Dechow, Ge, Larson, and Sloan (2011). We require these events to happen within one year before or after the restatement.

The third criterion is restatements that involve Rule 10b-5 allegations of fraud, both in cases brought by the SEC and in security class action lawsuits. A Rule 10b-5 allegation requires scienter (Choi and Pritchard 2016) and thus represents a category of misstatements with allegations of intentional fraud. For class action lawsuits, we require that the case not be dismissed or terminated. We also require a related AAER period to overlap with the periods restated for the SEC cases. For the security class action lawsuits, we require the class period to overlap with the periods restated. In each case, we read legal summaries to confirm that allegations involve earnings misstatements. We exclude two categories of restatements from the irregularity group—lease restatements and option backdating restatements—as both are
less likely to be intentional.\textsuperscript{4}

For our main specification, we combine revenue recognition and irregularity restatements. Finally, for all restatements, we require that misstatements have a nonzero net income effect over restated period. This requirement is important because in the estimation, we set the bias in book value equal to the cumulative impact of a restatement on net income. Finally, we only keep restatements that correct annual financial statements.

### 3.2 Subsample construction

Our sample period covers one significant change in disclosure regulation—the Sarbanes-Oxley Act (SOX), which constituted major disclosure regulation. Section 302 requires CEOs and CFOs to certify financial statements and establishes CEOs and CFOs as having direct responsibility for the accuracy of financial reports and internal controls over financial reporting. Section 404[a] requires management certification of internal controls over financial reporting. The first year of Section 404[a] compliance for smaller companies was 2007. Section 404[b] requires auditors to attest to the management’s assessment of internal controls. U.S. accelerated filers had to implement Section 404[b] after November 15, 2004.

This legislation and concurrent events have changed the expected cost of manipulation, both in terms of detection probability and penalty. Accordingly, there are two distinct regimes that can affect the misstatement cost parameters: the pre-SOX period ending in August 2002 and the post-SOX period.

We estimate our model on the subsample with the longest time span, the post-SOX period.

\textsuperscript{4}In the Audit Analytics taxonomy, lease restatements correspond to the categories 21 (Lease SFAS 5 legal contingency and commitment issues) and 42 (Lease leasehold and FAS 13 98 only subcategory). Option backdating corresponds to categories 17 (Deferred stock-based and/or executive compensation issues) and 48 (Deferred stock-based options backdating only subcategory).
3.3 Summary statistics

Because the patterns in descriptive statistics are similar for the SG&A and R&D samples, the discussion below focuses on the SG&A sample. Figure 3 plots the incidence of restatements and the corresponding rate of restated annual periods by year. These two quantities are not identical because when a restatement occurs, financial statements from several previous years are often corrected at the same time. The incidence of restatements increases dramatically right after the passage of SOX and peaks after the SOX Section 404 implementation of internal control disclosures in 2004 (Whalen, Usvyatsky, and Tanona 2016). Incidence steadily declines thereafter. This pattern is consistent with detection probability increasing in the post-SOX period. Because of the backward-looking nature of restatements, the rate of restated annual periods also declines over time.

Figure 4 plots the ratio of the bias in earnings to sales as a function of time. Because the cost of manipulation increases over this time period, the magnitude of earnings misstatements naturally declines over time.

Table 2 (panel A) provides descriptive statistics for restatements, CEO compensation, and firm characteristics for the SG&A sample. For the combined sample of restatements, the mean (median) bias in book value is $51.2 ($3.5) million or 4.4% (0.7%) of sales. The corresponding bias in earnings is $13.7 ($1.1) million or 2.9% (0.2%) of sales. For the irregularity restatements, the mean (median) bias in book value is $73.6 ($5.9) million or -5.6% (0.9%) of sales. The corresponding bias in earnings is $19.6 ($1.7) million or 2.7% (0.2%) of sales.

This table also provides descriptive statistics for the CEO’s equity holdings. In line with the evidence in Frydman and Jenter (2010), the mean (median) CEO holds 5.2% (0.8%) of all outstanding stock.

Finally, Table 2 provides descriptive statistics for the variables used in estimation, as well as other firm characteristics. Recall that many of our moments are growth rates, which we compute as differences relative to the absolute value of an average following Davis and
Haltiwanger (1992) and Terry (2015). For instance, the one-year growth in $x_t$ is computed as

$$
\Delta x = \begin{cases} 
0, & x_t = 0 \text{ and } x_{t-1} = 0, \\
2 \frac{x_t - x_{t-1}}{|x_t| + |x_{t-1}|}, & \text{otherwise.}
\end{cases}
$$

(13)

These growth rates have the advantage of being bounded within $[-2; 2]$. This restriction is important because often variables shift from zero to nonzero values, so, for example, the shift from zero to positive R&D investment results in a finite rather than a missing value.

The mean one-year growth in cash flows is 4.2%, the one-year growth in earnings is 5.0%, the one-year growth in SG&A is 7.1%, the one-year growth in R&D is 6.0% and the three-year growth in sales is 22.9%. Because this last figure is quite large, and because it likely reflects not only greenfield growth but also mergers, entry, and exit, we use a sales weighted growth rate in our $\xi$-matching algorithm described above. Finally, the firms in our sample are identical in size to a generic Compustat sample. The mean firm assets are $2.97$ billion in our sample, while the mean assets of all firms in Compustat over the same period is $2.52$ billion.

## 4. Estimation

We first set the discount rate, $r$, to 6%. This figure represents a premium over the 3.84% average ten-year Treasury bond over our sample period, and it is generally consistent with evidence that managers set discount rates higher than one would predict using a standard model (Graham and Harvey 2001). We also note that the fraction of manager dividend claims $\theta_d > 0$ exchanges units with the manager’s incentives to meet or beat earnings $\theta_f$, and without loss of generality we normalize $\theta_d = 1$.

We also estimate two parameters separately: the innovation productivity shifter, $\xi$, and the rate of earnings conversion to cash flows, $\hat{p}_s$. The parameter $\xi$ shifts the innovation production function and thus maps strongly and positively into the mean growth rate, $E_y \Delta_3 y$, which is computed as the sales-weighted three-year growth rate of sales, given by
\[ \mathbb{E}_y (y_{i,t-3} \Delta_3 y_{i,t}) / \mathbb{E}_y (y_{i,t-3}), \text{ with } \Delta_3 y_{i,t} = 2(y_{i,t} - y_{i,t-3}) / (y_{i,t} + y_{i,t-3}). \] An estimate of the parameter \( \xi \) directly affects the estimates of the growth implications of our model. Because having an accurate estimate of \( \xi \) is important for our main results, we target the moment \( \mathbb{E}_y \Delta_3 y \) exactly in the bisection procedure for \( \xi \) described above in our discussion of the model solution.

To estimate the rate of earnings conversion to cash flows, we follow the accounting literature and estimate \( \hat{p}_s \) from a regression of earnings, \( \pi_t \), on past, future, and current cash flows, \( d_t \), with all variables scaled by average total assets. Specifically, we estimate \( \hat{p}_s \) as the average of \( \beta_{t-1} \) and \( \beta_{t+1} \) from the following regression

\[
\pi_t = \alpha + \beta_{t-1} d_{t-1} + \beta_t d_t + \beta_{t+1} d_{t+1} + v_t, \tag{14}
\]

which is similar but not identical to the specification in Dechow and Dichev (2002). Because cash collection and disbursement policies can be firm- and year-specific, we include firm and year fixed effects in this regression. For the post-SOX SG&A sample, \( \hat{p}_s \) equals 18%, that is, 18% of earnings get collected in cash in the preceding or following years.

We estimate the model’s remaining parameters using a simulated minimum distance estimator, where we need to simulate because of the presence of the earnings reshuffling shock, \( \zeta_{it} \). The mechanics of the estimation are straightforward and by now familiar (Bazdresch, Kahn, and Whited 2018). For a given set of parameters, we solve the model and use the solution to generate simulated data, which is ten times the size of our data set (Michaelides and Ng 2000). Next, we calculate a set of statistics, which are either moments or functions of moments. Based on the distance between model-generated statistics and their empirical counterparts, the values of the structural parameters are updated. To gauge this distance, we use the inverse covariance matrix of the empirical moments. To minimize the econometric objective function, we use a global stochastic optimization routine.
4.1 Identification

We have nine remaining model parameters to estimate: $p_w$, the relative price of intangible investment; $\gamma$, the elasticity of innovation to investment; $\rho_{y}$ and $\sigma_{y}$, the persistence and volatility of the fundamental shock; $\sigma_{\pi}$, the volatility of the non-fundamental shock to profits; $\kappa_{f}$ and $\kappa_{q}$, the fixed and quadratic costs of manipulation, conditional upon discovery; $\lambda$, the probability of manipulation discovery, and $\theta_f$, the manager’s incentive to report earnings growth.

To identify these parameters, we use 21 moment conditions. The first seven of these moments do not rely on manipulation data. The first is the mean ratio of intangible investment to sales, given by $E(p_w w/y)$. The next three moments are variances. The first of these is the variance of observed dividend growth, $\Delta d$, defined as $\Delta d = 2(d - d_{-1})/(d + d_{-1})$. The next two variances are those of the growth rates of reported earnings, $\Delta \pi$, and intangible investment, $\Delta w$, which are defined similarly. The next three moments are covariances, in particular, the three possible covariances between $\Delta d$, $\Delta \pi$, and $\Delta w$.

The remaining 14 moments relate directly to manipulation and detection events. We include the probability of detection, $E(I_D)$, in which the dummy variable, $I_D$, indicates the actual discovery of manipulation in a period. We also target the mean absolute ratio of manipulation to sales, conditional upon detection, $E(|b/y| | I_D)$, as well as the variance and skewness of the same manipulation ratio conditional upon detection.

To allow for the possibility that misreporting firms behave differently from non-misreporting firms, we also duplicate the covariance matrix of dividend growth, $\Delta d$, earnings growth, $\Delta \pi$, and intangible investment growth, $\Delta w$, except that we condition upon detection. Finally, since the magnitude of the change in bias $b - b_{-1}$ – the term which directly shifts today’s earnings – is observable in detection events, we also add the series $\Delta(b - b_{-1})$, i.e., the growth rate of today’s earnings bias level, into the covariance matrix conditional upon detection.

While each of these moments is related to nearly all the parameters in the model, some moments have strong monotonic relationships with certain parameters and are thus particularly
useful for identifying those parameters. To ascertain the strength of these relationships, we perform a battery of comparative statics exercises, which we then use to justify our moment choices.

We start with technological parameters. The first technological parameter is the price of intangible investment, \( p_w \). This parameter determines the costliness of intangible investment in terms of the numeraire output and thus maps directly into the size of intangible investment \( E(p_w w/y) \). The second technological parameter is \( \gamma \), which governs the returns to intangible investment in the innovation equation (2). Intuitively, when this parameter is higher, intangible investment responds more strongly to shocks, so a high level for \( \gamma \) results in high covariances between intangible investment and indicators of fundamentals, in particular, dividends and earnings, both unconditionally and conditional upon detection. Naturally, if investment is more responsive, it also has a higher variance, so \( \gamma \) also affects this moment.

Next, we consider the persistence of the fundamental shock, \( \rho_y \). This parameter affects many different moments. In particular, \( \rho_y \) maps negatively into the volatility of all growth rates in the model for the simple reason that a high slope coefficient in an \( AR(1) \) process maps into a low process variance. This negative relation holds for all the growth rate volatility moments, both unconditionally and conditional upon detection. A separate, less mechanical effect is also at work. Because higher fundamental persistence makes today’s fundamental shock more informative for tomorrow, the covariance between the output shock and investment increases. This effect leads to a higher covariance between dividend and investment growth. Because accruals manipulation allows the manager to choose a more fundamentals-aligned investment level without sacrificing earnings, this last effect is more pronounced when manipulation is discovered.

Unlike the persistence parameter, \( \rho_y \), the volatility of the fundamental shock, \( \sigma_y \), is a neutral volatility shifter that primarily affects observable growth rate variances. Although \( \sigma_y \) mechanically affects covariances, these effects are small relative to the effects on volatilities.

The identification of the volatility of our nonfundamental earnings shock, \( \sigma_\pi \), operates
somewhat differently. First, we have a strong, mechanical, positive link between this parameter and the variance of earnings, both unconditionally and conditional upon detection. However, the volatility of non-fundamental shocks also maps into the volatility of investment, as long as there is motive for real manipulation, which in our model takes the form of pressure to deliver short-term earnings growth. Naturally, this mapping is weaker when punishment of accruals-based manipulation, embodied in $\kappa_f$ and $\kappa_q$ is present.

Next, we consider the manipulation cost parameters, starting with the quadratic cost parameter, $\kappa_q$. This parameter determines the costliness of accruals manipulation on the intensive margin, so the mean absolute ratio of manipulation to sales, conditional upon detection, decreases in $\kappa_q$, as does the variance of bias upon detection. In addition, when accruals manipulation is more costly, more manipulation occurs through investment, so the variance of investment growth increases. Finally, a higher cost reduces the covariance between investment and dividend growth, as investment becomes a tool with which to respond to non-fundamental shocks.

Our second manipulation cost parameter, $\kappa_f$, quantifies the fixed costs of manipulation, conditional upon detection of manipulation. As such, this parameter determines the cost of accruals manipulation at the extensive margin. Mechanically, a higher fixed cost of discovery of manipulation leads to a lower probability of manipulation and hence detection, so the probability of detection is lower. Note, however, that the detection probability is also driven in large part by the random detection likelihood parameter $\lambda$, which maps more strongly into detection, $\mathbb{E}(I_D)$, relative to the $\kappa_f$ parameter. A second effect operates through increasing returns to manipulation, which naturally arises in the presence of a fixed cost. In this case, manipulation does not occur unless it is highly worth it, so a high fixed cost implies a higher average bias, $\mathbb{E}(|b/y| \mid I_D)$ as well as a larger magnitude of the skewness of bias given detection.

Both parameters, $\kappa_f$ and $\kappa_q$, affect the magnitude of detected manipulation. However, their separate identification hinges on their differential effects on the variance and skewness of the absolute ratio of manipulation to sales, conditional upon detection moments. If $\kappa_q$
were near zero and \( \kappa_f \) were high, then the magnitude of the manipulation would have higher skewness, as the firm would optimally manipulate infrequently, but it would manipulate a great deal when it did. Conversely, if \( \kappa_q \) were high and \( \kappa_f \) were zero, the distribution of manipulation would be much more symmetric, so skewness should depend on the relative magnitudes of \( \kappa_q \) and \( \kappa_f \). A similar argument applies to the variance of manipulation.

The probability of detection, \( \lambda \), governs the likelihood of the discovery of manipulation, which is a Poisson-style shock in the model. Mechanically, the observed likelihood of detection goes up, but because firms internalize the likelihood of discovery in their manipulation choices, the amount of manipulation increases less. Moreover, the slope of each of these mappings increases with \( \kappa_f \).

The magnitude of managers’ incentive to meet their lagged profit benchmark, \( \theta_f \), changes the manner in which R&D investment relates to firm dividend and profit flows. When \( \theta_f = 0 \) and managers face no manipulation incentives, persistent fundamental shocks \( \nu_y \) tend to push dividend and profit flows in the same direction as investment. However, when managers face stronger incentives to beat earnings benchmarks with higher levels of \( \theta_f \), then managers will sometimes cut their R&D after unlucky shocks in order to maintain profit growth. The result is a lower - in severe enough cases negative - covariance between investment growth and both dividend and profit growth. Naturally, since investment is used as a smoothing tool for profits, the volatility of investment growth also rises with higher \( \theta_f \).

5. Estimation results and counterfactuals

The results from our estimation using the SG&A sample are in Table 3. In Panel A, we report the actual data moments, the model-simulated moments, and \( t \)-statistics for the null of the equality of each pair of moments. While most of the moment pairs are insignificantly different from each other, few are economically different, and several of these pairs match up nicely. Overall, however, we believe the fit of the model is remarkably good, given that we have a high degree of overidentification. Accordingly, it is a useful laboratory for counterfactual
policy experiments.

Next, we turn to the parameter estimates, which are reported in Panel B. These parameters divide naturally into two groups, reflecting firm fundamentals on the one hand and income reporting or manager incentives on the other hand. Turning to the first group of parameter estimates, the implied fundamentals for firms are in line with many of the extant estimates in the literature. Intangible investment has a relative price of above one with $\hat{p}_w \approx 3.2$, reflecting a higher cost of intangible investment relative to numeraire output. The persistence of productivity or profitability of $\hat{\rho} \approx 0.36$ lies below the level of the estimated persistence of productivity in all U.S. firms estimated by Winberry (2016) ($\approx 0.78$) or in U.S. manufacturing estimated by Castro, Clementi, and Lee (2015) ($\approx 0.45$). This result is to be expected because our model of growth at the firm level endogenizes a meaningful amount of persistence at firms through accumulation of the intangible asset rather than relying on the exogenous process for such persistence as in a wide range of commonly used stationary models of firm dynamics. The total conditional volatility of shocks to firm profitability each year is $\sum \hat{\sigma}_y^2 + \hat{\sigma}_\pi^2 \approx 0.41$, which is slightly higher than the total volatility of shocks to U.S. public firms estimated by studies that omit a role for non-fundamental shocks such as Gourio and Rudanko (2014). Finally, the estimated elasticity of innovation to intangible investments $\hat{\gamma} \approx 0.37$ lies well below one, consistent with the evidence from patenting, firm growth, and R&D in papers including Acemoglu, Akcigit, Bloom, and Kerr (2013). The parameters governing reporting and earnings growth incentives for the manager, $\kappa_q$, $\kappa_f$, and $\theta_f$ mostly relate to manager preferences and lack a direct empirical equivalent. One exception is the probability of detection $\hat{\lambda} \approx 0.11$, which compares well to the estimates from a similar dynamic model in Zakolyukina (forthcoming). Overall, the parameters in Table 3 appear reasonable.

5.1 The dynamics of restatement and intangible investment

The model provides incentives to managers to shift reported profits upwards in periods when doing so ensures profit growth. Managers have two tools with which they can achieve this
upward manipulation, biased reporting or real investment shifts, and each tool is costly at the margin. The direct implication within the model is that managers will use both levers to manipulate their earnings upward in such periods, leading to a positive shift in bias as well as a lower level of intangible investment. Empirically, Figure 1 displayed exactly this pattern. But does the empirical result hold up when estimated off of simulated model data? We then run the panel regressions in simulated data:

$$X_{jt} = \sum_{k=-K}^{K} \beta_k I(\text{Upward Bias Restated})_{jt+k} + \varepsilon_{jt}.$$  

To match our empirical approach in the construction of Figure 1, $X_{jt}$ is either the R&D to sales ratio in the model (left panel) or the bias to sales ratio (right panel). In Figure 5, we plot the coefficients $\beta_k$, which trace out the within-firm idiosyncratic variation in intangible investment at horizons $k$ periods away from the restatement event. The red line on the left-hand side plots the resulting dynamics of R&D in the data, and we see a quick drop in R&D of around 5% for the firm in periods in which upward bias is restated, labelled “0.” On the right-hand side, we see upward manipulation of reported earnings by a bit more than 5% on average.

The dynamic patterns in the data in Figure 1 were untargeted, and their model counterparts in Figure 5 are not too far off in magnitude. The qualitative message in both cases is also clear. Managers cut their investment in periods in which they have upwardly misreported profits. Examination of each plot in Figure 1 and Figure 5 also reveals that the model and data dynamics match along another untargeted dimension, the transitory nature of the associated R&D declines. In the model, R&D rebounds quickly because of the short-lived nature of opportunities for manipulation. The transitory observed fluctuation in R&D is not an extraneous feature of the model. Instead, mismatch between the short-term variation in incentives to manipulate long-term investment, on the one hand, and more persistent variation in incentives to invest, on the other hand, drive the efficiency loss for firms in a context with real investment manipulation.

31
5.2 Counterfactuals

In the presence of short-term incentives to grow earnings, managers face pressure to manipulate their reported earnings using one of two available tools: real investment choices or bias in reporting. Reporting is subject to convex costs upon discovery, and large manipulation of investment leads to more costly deviations from a value maximizing benchmark. Therefore, managers in general will substitute across the two different forms of manipulation, shifting their investment only moderately while simultaneously introducing some bias in their reporting. The result, of course, is a classic trade-off. Managers facing higher cost of biased reporting will release more accurate income statements but choose less efficient, and more volatile, investment paths.

In Table 4, we quantify these trade-offs based on a series of counterfactual calculations, reporting a set of results based on the baseline estimated model and a model with no reporting bias, and a value-maximizing firm for comparison. We compute these counterfactuals based on the sets of parameter estimates from Table 3. The first column of the table reports that managers in the baseline estimated model in equilibrium choose reporting bias equal to around 3% of sales, conditional upon restatement. A manager facing infinite costs of misreporting in the second column, and choosing no bias, clearly releases more accurate income statements. The second row emphasizes the trade-off discussed above. Because managers without the ability to misreport their profits choose to manipulate through their investment alone, the growth rate declines by around 5 basis points, a meaningful drop relative to small average growth rates overall. Distortions to the path of investment lead to a loss in the underlying or fundamental firm value, and the third row reports that eliminating bias in income statements from the estimated equilibrium would cost a bit under 1% of firm value on average. Finally, in the third column we consider an environment with no earnings manipulation incentives and value maximization. While not necessarily achievable in practice, this environment naturally results in improvements in firm growth and bias.

The counterfactual cases considered in Table 4 are informative but extreme. Figure 6 plots
the equilibrium trade-off between investment efficiency and bias in reporting as the cost of bias \( \kappa_q \) varies more moderately. As the costs of manipulation decline, average bias increases inversely on the horizontal axis, but investment efficiency improves, as reflected in improved firm value, on the vertical axis. Starting from the empirical magnitude of bias in the data, indicated with the circular marker on the figure, a further reduction in bias can be achieved only through reductions in average firm value. Policymakers concerned with both the accuracy of income reporting and the real efficiency of firms must take the quantitative magnitude of this trade-off, which constrains their choices, into account when designing reporting regulation.

6. Conclusion

We quantify the importance of managers’ opportunistic distortion of information to the public as a force that improves the efficiency of their investment choices. While it is counterintuitive to imagine that less information could lead to better real outcomes, this seemingly counterintuitive connection makes sense in the context of widespread short-term incentives. On the one hand, many features of compensation contracts, such as performance-based equity compensation and bonus plans, give managers the incentive to manipulate earnings disclosures. On the other hand, disclosure or misreporting regulation does not erase these incentives, so when managers find it costly to misreport earnings, they substitute opportunistic cuts to investment, which can have adverse effects on shareholder value. Indeed, survey evidence suggests that managers facing pressures to report high earnings numbers appear to both misreport their earnings and distort long-term investments (Graham et al. 2005). If managers are willing to substitute between these two forms of manipulation, then reforms either to reporting regulations or executive compensation may face a crucial trade-off between the accuracy of information reported by firms and the efficiency of long-term investment (Cohen et al. 2008).

However, given the scale of recent reforms to firm disclosure regulations, e.g. the Sarbanes-Oxley Act in the United States, quantifying the extent of this trade-off seems crucial. Our vehicle for addressing this question is estimation of a dynamic model that incorporates all the
ingredients necessary to generate the trade-off between misreporting and investment efficiency: an incentive structure with both short-term and long-term incentives, persistent investment opportunities that enhance firm growth, and punishment for misreporting. Because the extent of misreporting, the payoffs to long-term investments, and the counterfactual response of firms to various policy and compensation regimes are difficult to measure with reduced-form exercises, our question requires estimating a dynamic model.

Our results are interesting and potentially useful for informing the debate over information disclosure regulation. Our model estimates imply that when managers are caught misreporting and forced to restate, their reporting bias equals around 3% of sales. In the model, if we make the cost of misreporting high, it disappears, but then managers mistime investment so that it does not occur when investment opportunities are best. This suboptimal behavior cuts shareholder value by almost 1%. The value loss from the existence of short-term incentives themselves is also meaningful, at about half a percent.

One ubiquitous drawback of our approach is the necessity of making model simplifications. For example, we only allow for one input into the production process, and the firm faces no financial frictions. We conjecture that advances in computing power will allow the specification of richer models to further our understanding of the little explored trade-offs between information manipulation, manager incentives, and the efficiency of the real economy.
References


Li, Chen, 2016, Mutual monitoring within top management teams: A structural modeling investigation, Manuscript, Baruch College.


Table 1: Data definitions

This table presents definitions and data sources for variables used in estimation. Compustat data codes are in parentheses.

<table>
<thead>
<tr>
<th>A. Firm-specific variables</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$\theta_d$</td>
<td>CEOs’ stock holdings (excluding options exercisable within 60 days) as a fraction of total shares outstanding. Equilar.</td>
</tr>
<tr>
<td>$y$</td>
<td>Sale revenues (SALE). Compustat.</td>
</tr>
<tr>
<td>$p_{w,w}$</td>
<td>Investment. For SG&amp;A sample, investment is XSGA; for R&amp;D sample, investment is XRD. Compustat.</td>
</tr>
<tr>
<td>$d$</td>
<td>Free cash flow is cash from operations (OANCF) minus net capital expenditures (CAPX - SPPE). Compustat.</td>
</tr>
<tr>
<td>$\pi$</td>
<td>Earnings is income before extraordinary items (IB). Compustat.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>B. Restatement-specific variables</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$I_D$</td>
<td>The indicator variable for detection that equals 1, when manipulation is detected and a firm restates its earnings. Audit Analytics advanced restatement feed.</td>
</tr>
<tr>
<td>$I_R$</td>
<td>The indicator variable that equals 1 in the years in which retained earnings were corrected by a restatement. Audit Analytics advanced restatement feed.</td>
</tr>
<tr>
<td>$b$</td>
<td>The bias in book value that equals the cumulative correction of net income. Audit Analytics advanced restatement feed.</td>
</tr>
</tbody>
</table>
This table presents descriptive statistics for the variables used in estimation. The sample is based on Equilar, Audit Analytics advanced restatements, and Compustat. The sample covers the period from 2000 to 2015 at an annual frequency. Compustat data codes are in parentheses. *Earnings* is income before extraordinary items (IB). *Free cash flow* is cash from operations (OANCF) minus capital expenditures (CAPX - SPPE). *R&D* is R&D expense (XRD) with missing values set to 0. *SG&A* is SG&A expense (XSGA) with missing values set to 0. *Market value* is the product of common shares outstanding (CSHO) and fiscal-year closing price (PRCC,F). *Total assets* is assets total (AT). *Sales* is sales revenue (SALE). *Market-to-book* is the sum of market value and total assets minus book value of equity divided by total assets. *Fiscal-year return* computed using fiscal-year closing stock prices. *Ownership* is the difference between shares owned (OWN_HOLDINGS) and options exercisable within 60 days (OWN_OPT_EX_60) divided by shares outstanding at fiscal-year end (SHARES_OUT_FY). *Bias in book value* is the cumulative change in restated net income. *Bias in earnings* is the change in restated net income. We exclude financial firms and utilities. All variables are winsorized at the 1st and 99th percentiles.

### A. SG&A sample

<table>
<thead>
<tr>
<th></th>
<th>Obs.</th>
<th>Mean</th>
<th>Std.Dev</th>
<th>p25</th>
<th>p50</th>
<th>p75</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bias in book value ($mn)</td>
<td>1,223</td>
<td>51.159</td>
<td>293.211</td>
<td>0.495</td>
<td>3.545</td>
<td>22.184</td>
</tr>
<tr>
<td>Bias in book value to sales</td>
<td>1,223</td>
<td>0.044</td>
<td>0.205</td>
<td>0.001</td>
<td>0.007</td>
<td>0.031</td>
</tr>
<tr>
<td>Bias in earnings ($mn)</td>
<td>1,223</td>
<td>13.712</td>
<td>182.680</td>
<td>0.000</td>
<td>1.118</td>
<td>6.402</td>
</tr>
<tr>
<td>Bias in earnings to sales</td>
<td>1,223</td>
<td>0.029</td>
<td>0.352</td>
<td>0.000</td>
<td>0.002</td>
<td>0.010</td>
</tr>
<tr>
<td>Annual bias in earnings growth</td>
<td>1,223</td>
<td>0.345</td>
<td>1.566</td>
<td>-1.127</td>
<td>0.468</td>
<td>2.000</td>
</tr>
<tr>
<td>Irregularities (N = 255)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Bias in book value ($mn)</td>
<td>801</td>
<td>73.602</td>
<td>359.303</td>
<td>0.752</td>
<td>5.864</td>
<td>33.796</td>
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<td>0.008</td>
<td>0.041</td>
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<td>Bias in earnings ($mn)</td>
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<td>1.665</td>
<td>10.170</td>
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<tr>
<td>Bias in earnings to sales</td>
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<td>0.027</td>
<td>0.293</td>
<td>0.000</td>
<td>0.002</td>
<td>0.013</td>
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<tr>
<td>Annual bias in earnings growth</td>
<td>801</td>
<td>0.342</td>
<td>1.551</td>
<td>-1.054</td>
<td>0.413</td>
<td>2.000</td>
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<td>CEO equity holdings (N = 3,565)</td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Ownership (%)</td>
<td>32,674</td>
<td>5.197</td>
<td>10.776</td>
<td>0.195</td>
<td>0.785</td>
<td>3.868</td>
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<tr>
<td>Firm characteristics (N = 3,565)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Obs.</td>
<td>32,674</td>
<td>11.734</td>
<td>4.287</td>
<td>8.000</td>
<td>13.000</td>
<td>16.000</td>
</tr>
<tr>
<td>Market value ($bn)</td>
<td>32,665</td>
<td>2.934</td>
<td>7.503</td>
<td>0.138</td>
<td>0.521</td>
<td>1.950</td>
</tr>
<tr>
<td>Total assets ($bn)</td>
<td>32,674</td>
<td>2.974</td>
<td>9.151</td>
<td>0.133</td>
<td>0.513</td>
<td>1.964</td>
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<tr>
<td>Sales ($bn)</td>
<td>32,674</td>
<td>2.425</td>
<td>5.919</td>
<td>0.120</td>
<td>0.485</td>
<td>1.776</td>
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<tr>
<td>Market-to-book</td>
<td>32,665</td>
<td>1.984</td>
<td>1.833</td>
<td>1.133</td>
<td>1.511</td>
<td>2.223</td>
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<tr>
<td>Fiscal-year return</td>
<td>32,630</td>
<td>0.168</td>
<td>0.713</td>
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<td>0.055</td>
<td>0.364</td>
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<td>Return on assets</td>
<td>32,674</td>
<td>-0.016</td>
<td>0.286</td>
<td>-0.019</td>
<td>0.037</td>
<td>0.077</td>
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<tr>
<td>SG&amp;A to sales</td>
<td>32,674</td>
<td>0.310</td>
<td>0.344</td>
<td>0.115</td>
<td>0.224</td>
<td>0.385</td>
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<tr>
<td>Annual free cash flow growth</td>
<td>32,674</td>
<td>0.042</td>
<td>1.182</td>
<td>-0.644</td>
<td>0.059</td>
<td>0.757</td>
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<td>Annual earnings growth</td>
<td>32,674</td>
<td>0.050</td>
<td>1.088</td>
<td>-0.453</td>
<td>0.106</td>
<td>0.579</td>
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<tr>
<td>Annual SG&amp;A growth</td>
<td>32,674</td>
<td>0.071</td>
<td>0.288</td>
<td>-0.021</td>
<td>0.056</td>
<td>0.150</td>
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<td>3-year sales growth</td>
<td>32,674</td>
<td>0.229</td>
<td>0.471</td>
<td>-0.014</td>
<td>0.209</td>
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</table>
### Table 2: —Continued

#### B. R&D sample

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<th>p25</th>
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<th>p75</th>
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</thead>
<tbody>
<tr>
<td>Bias in book value ($mn)</td>
<td>691</td>
<td>56.004</td>
<td>269.326</td>
<td>0.404</td>
<td>3.049</td>
</tr>
<tr>
<td>Bias in book value to sales</td>
<td>691</td>
<td>0.060</td>
<td>0.263</td>
<td>0.001</td>
<td>0.008</td>
</tr>
<tr>
<td>Bias in earnings ($mn)</td>
<td>691</td>
<td>15.674</td>
<td>120.323</td>
<td>-0.032</td>
<td>1.038</td>
</tr>
<tr>
<td>Bias in earnings to sales</td>
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<td>0.046</td>
<td>0.466</td>
<td>-0.000</td>
<td>0.002</td>
</tr>
<tr>
<td>Annual bias in earnings growth</td>
<td>691</td>
<td>0.342</td>
<td>1.581</td>
<td>-1.188</td>
<td>0.501</td>
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#### Irregularities (N = 152)

<table>
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<th>p25</th>
<th>p50</th>
<th>p75</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bias in book value ($mn)</td>
<td>483</td>
<td>75.824</td>
<td>319.336</td>
<td>0.446</td>
<td>5.113</td>
</tr>
<tr>
<td>Bias in book value to sales</td>
<td>483</td>
<td>-0.112</td>
<td>3.860</td>
<td>0.001</td>
<td>0.009</td>
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<tr>
<td>Bias in earnings ($mn)</td>
<td>483</td>
<td>21.130</td>
<td>143.168</td>
<td>-0.030</td>
<td>1.666</td>
</tr>
<tr>
<td>Bias in earnings to sales</td>
<td>483</td>
<td>0.040</td>
<td>0.374</td>
<td>-0.000</td>
<td>0.003</td>
</tr>
<tr>
<td>Annual bias in earnings growth</td>
<td>483</td>
<td>0.312</td>
<td>1.568</td>
<td>-1.137</td>
<td>0.352</td>
</tr>
</tbody>
</table>

#### CEO equity holdings (N = 2,133)

<table>
<thead>
<tr>
<th>Obs.</th>
<th>Mean</th>
<th>Std.Dev</th>
<th>p25</th>
<th>p50</th>
<th>p75</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ownership (%)</td>
<td>19,444</td>
<td>3.970</td>
<td>8.741</td>
<td>0.154</td>
<td>0.629</td>
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</tbody>
</table>

#### Firm characteristics (N = 2,133)

<table>
<thead>
<tr>
<th>Obs.</th>
<th>Mean</th>
<th>Std.Dev</th>
<th>p25</th>
<th>p50</th>
<th>p75</th>
</tr>
</thead>
<tbody>
<tr>
<td>Market value ($bn)</td>
<td>19,444</td>
<td>11.695</td>
<td>4.290</td>
<td>8.000</td>
<td>13.000</td>
</tr>
<tr>
<td>Total assets ($bn)</td>
<td>19,444</td>
<td>3.204</td>
<td>8.360</td>
<td>0.125</td>
<td>0.475</td>
</tr>
<tr>
<td>Sales ($bn)</td>
<td>19,444</td>
<td>2.932</td>
<td>10.225</td>
<td>0.091</td>
<td>0.362</td>
</tr>
<tr>
<td>Market-to-book</td>
<td>19,444</td>
<td>2.182</td>
<td>6.012</td>
<td>0.066</td>
<td>0.295</td>
</tr>
<tr>
<td>Fiscal-year return</td>
<td>19,444</td>
<td>2.311</td>
<td>2.291</td>
<td>1.240</td>
<td>1.711</td>
</tr>
<tr>
<td>Return on assets</td>
<td>19,444</td>
<td>0.169</td>
<td>0.741</td>
<td>-0.237</td>
<td>0.048</td>
</tr>
<tr>
<td>R&amp;D to sales</td>
<td>19,444</td>
<td>-0.061</td>
<td>0.374</td>
<td>-0.064</td>
<td>0.031</td>
</tr>
<tr>
<td>Annual free cash flow growth</td>
<td>19,444</td>
<td>0.064</td>
<td>2.919</td>
<td>0.013</td>
<td>0.056</td>
</tr>
<tr>
<td>Annual earnings growth</td>
<td>19,444</td>
<td>0.056</td>
<td>1.089</td>
<td>-0.471</td>
<td>0.100</td>
</tr>
<tr>
<td>Annual R&amp;D growth</td>
<td>19,444</td>
<td>0.060</td>
<td>0.409</td>
<td>-0.060</td>
<td>0.044</td>
</tr>
<tr>
<td>3-year sales growth</td>
<td>19,444</td>
<td>0.219</td>
<td>0.531</td>
<td>-0.037</td>
<td>0.204</td>
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</table>
Table 3: Baseline estimation results: SG&A

A. Moments

<table>
<thead>
<tr>
<th></th>
<th>Simulated moments</th>
<th>Data moments</th>
<th>t-statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean ratio of SG&amp;A to sales</td>
<td>0.3144</td>
<td>0.3228</td>
<td>-5.1003</td>
</tr>
<tr>
<td>Incidence of detection</td>
<td>0.0120</td>
<td>0.0115</td>
<td>1.7623</td>
</tr>
<tr>
<td>Mean absolute bias relative to sales, given detection</td>
<td>0.0710</td>
<td>0.0689</td>
<td>0.1652</td>
</tr>
<tr>
<td>Variance of dividend growth</td>
<td>1.2931</td>
<td>0.3335</td>
<td>7.3895</td>
</tr>
<tr>
<td>Covariance of dividend and earnings growth</td>
<td>0.2624</td>
<td>0.2942</td>
<td>-2.7640</td>
</tr>
<tr>
<td>Covariance of dividend and R&amp;D growth</td>
<td>-0.0108</td>
<td>-0.0242</td>
<td>3.5139</td>
</tr>
<tr>
<td>Variance of earnings growth</td>
<td>1.0980</td>
<td>0.8743</td>
<td>2.1364</td>
</tr>
<tr>
<td>Covariance of earnings and R&amp;D growth</td>
<td>-0.0094</td>
<td>-0.0113</td>
<td>2.5962</td>
</tr>
<tr>
<td>Variance of R&amp;D growth</td>
<td>0.0678</td>
<td>0.0864</td>
<td>-9.8537</td>
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<tr>
<td>Variance of dividend growth, given detection</td>
<td>1.6599</td>
<td>0.2054</td>
<td>13.9137</td>
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<tr>
<td>Covariance of dividend and earnings growth, given detection</td>
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<td>0.0083</td>
<td>3.3104</td>
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<td>Covariance of dividend and R&amp;D growth, given detection</td>
<td>-0.0286</td>
<td>-0.0046</td>
<td>-1.5336</td>
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<tr>
<td>Covariance of dividend and earnings bias growth, given detection</td>
<td>0.0079</td>
<td>0.0135</td>
<td>-0.0481</td>
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<tr>
<td>Variance of earnings growth, given detection</td>
<td>1.2527</td>
<td>0.0293</td>
<td>13.7880</td>
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<tr>
<td>Covariance of earnings and R&amp;D growth, given detection</td>
<td>-0.0217</td>
<td>-0.0017</td>
<td>-1.1954</td>
</tr>
<tr>
<td>Covariance of earnings and earnings bias growth, given detection</td>
<td>0.2126</td>
<td>0.0050</td>
<td>2.0732</td>
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<tr>
<td>Variance of R&amp;D growth, given detection</td>
<td>0.0641</td>
<td>0.0890</td>
<td>-1.3759</td>
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<tr>
<td>Covariance of R&amp;D growth and earnings bias growth, given detection</td>
<td>0.0058</td>
<td>-0.1726</td>
<td>9.5441</td>
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<tr>
<td>Variance of earnings bias growth, given detection</td>
<td>2.3322</td>
<td>0.5380</td>
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<tr>
<td>Variance of absolute bias, given detection</td>
<td>0.0514</td>
<td>0.0013</td>
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<tr>
<td>Skewness of absolute bias, given detection</td>
<td>6.3146</td>
<td>2.1695</td>
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B. Parameter estimates

<table>
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<tr>
<th>$p_w$</th>
<th>$\rho_y$</th>
<th>$\sigma_y$</th>
<th>$\sigma_\pi$</th>
<th>$\kappa_q$</th>
<th>$\kappa_f$</th>
<th>$\gamma$</th>
<th>$\lambda$</th>
<th>$\theta_f$</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.1789</td>
<td>0.3595</td>
<td>0.3193</td>
<td>0.2595</td>
<td>36.5760</td>
<td>0.0062</td>
<td>0.3661</td>
<td>0.1117</td>
<td>0.1379</td>
</tr>
<tr>
<td>(0.0571)</td>
<td>(0.0154)</td>
<td>(0.0018)</td>
<td>(0.0020)</td>
<td>(10.6526)</td>
<td>(0.0195)</td>
<td>(0.0069)</td>
<td>(0.0423)</td>
<td>(0.0075)</td>
</tr>
</tbody>
</table>

The estimation is done with simulated minimum distance, which chooses structural model parameters by matching the moments from a simulated panel of firms to the corresponding moments from the data. Panel A reports the simulated and actual moments. Panel B reports the estimated structural parameters. $p_w$ is the price of R&D relative to output. $\rho_y$ is the serial correlation of the persistent productivity shock. $\sigma_y$ is the volatility of the persistent productivity shock. $\sigma_\pi$ is the volatility of the i.i.d. shock to earnings. $\kappa_q$ is the quadratic cost of manipulation. $\kappa_f$ is the fixed cost of manipulation. $\gamma$ is the curvature of the innovation production function. $\lambda$ is the probability of manipulation detection. $\theta_f$ is the manager incentive to beat lagged profits.
Table 4: Bias vs. value: counterfactual experiments

<table>
<thead>
<tr>
<th>Model</th>
<th>Baseline (Estimated)</th>
<th>No Bias ($\kappa_q = \kappa_f = \infty$)</th>
<th>Value Maximizing ($\theta_f = 0$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean Bias, %</td>
<td>2.88</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>Mean Growth, %</td>
<td>3.33</td>
<td>3.28</td>
<td>3.43</td>
</tr>
<tr>
<td>Firm Value Change from Baseline, %</td>
<td>0.00</td>
<td>-0.83</td>
<td>0.49</td>
</tr>
</tbody>
</table>

The table reports various outcomes computed under three alternative model parameterizations. The first column reports moments from the baseline model (with estimated parameters), the second column reports moments a model with no accounting bias (identical to baseline with bias costs $\kappa_q, \kappa_f$ set to $\infty$), and the third column reports moments from a value maximizing model with no earnings growth incentives (identical to baseline with earnings incentive parameter $\theta_f = 0$). The first row reports the mean bias relative to sales conditional upon restatement. The second row reports the mean growth of firm quality. The third row reports the average change in fundamental firm value relative to the baseline model. All counterfactual moments are computed using the ergodic distribution of the respective models, with all units in percent except for the already normalized correlation moment.
The figure plots the dynamics of intangible investment (left panel) and reporting bias (right panel) around firm restatement events in which earnings were biased upwards. In particular, each solid line in the figure plots estimated coefficients $\beta_k$, $k = -K,...,K$ from the panel regression $X_{jt} = \sum_{k=-K}^{K} \beta_k I(Upward Bias Restated)_{jt+k} + f_s + g_t + \varepsilon_{jt}$. For firm $j$ at time $t$ in sector $s$, the variable $X$ is selling, general, and administrative expenditures (left hand side) and reported bias in book value, both relative to sales. A full set of sector and time dummies together with indicators for public restatement of an upward bias in profits for firm $j$ at the horizon $k$ from year $t$ is included. We use $K = 2$ for the figure estimates. The plotted error bands are 95% confidence intervals, clustered by firm.
Figure 2: Investment and bias in the estimated model

Each panel of the figure plots a firm policy function - for their choice of investment (top row) or bias (bottom row) - in the estimated baseline model as a function of the fundamental shock $v_y$ (left column) and the non-fundamental profit shock $\nu_\pi$ (right column). The top row plots a firm’s investment policy in percent deviations from the mean investment policy in the model. The bottom row plots a firm’s bias policy $b$ as a percent of mean sales. The plotted policy functions are smoothed averages over the ergodic distribution of the model, conditioning upon the indicated values of the fundamental and profit shocks.
Figure 3: Incidence of misreporting

This figure depicts restatement rate and restated annual financial statements by year for revenue recognition and irregularity restatements in SG&A sample.
Figure 4: Magnitude of misreporting

This figure depicts the ratio of the bias in earnings to sales as a function of time for revenue recognition and irregularity restatements in SG&A sample.
Figure 5: Dynamics around a restatement event - simulated data

The figure plots the dynamics of intangible investment (left panel) and reporting bias (right panel) around firm restatement events in which earnings were biased upwards. In particular, each solid line in the figure plots estimated coefficients $\beta_k$, $k = -K, ..., K$ from the panel regression $X_{jt} = \sum_{k=-K}^{K} \beta_k I(\text{Upward Bias Restated})_{jt+k} + \varepsilon_{jt}$. For firm $j$ at time $t$, the variable $X$ is R&D expenditures (left hand side) and reported bias in book value, both relative to sales. We use $K = 2$ for the figure estimates. The plotted error bands are 95% confidence intervals, clustered by firm.
Figure 6: Tradeoffs

The figure plots the equilibrium average change in firm value (on the vertical axis) and average bias relative to sales in restatements (on the horizontal axis). Each point on the curve reports moments from a counterfactual experiment, starting from the baseline estimated parameterization of the model and changing only the manager’s cost of bias $\kappa_q$ either up or down. The curve is a polynomial interpolation of moments from a discrete set of counterfactual experiments. The empirical magnitude of bias is indicated by the black circular dot, and all value change figures are expressed relative to this point.